# Corporate earnings and the equity premium ${ }^{\text {ts }}$ 

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#### Abstract

Corporate cash flows are highly volatile and strongly procyclical. We examine the assetpricing implications of the sensitivity of corporate cash flows to economic shocks within a continuous-time model in which dividends are a stochastic fraction of aggregate consumption. We provide closed-form solutions for stock values and show that the equity premium can be represented as the sum of three components which we call the consumption-risk, event-risk, and corporate-risk premia. Calibrated to historical data, the model implies a total equity premium many times larger than in the standard model. The model also generates levels of equity volatility consistent with those experienced in the stock market.


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## 1. Introduction

Standard asset-pricing theory implies that equilibrium asset values can be expressed as the expected product of a pricing kernel and the cash flows from those assets. The ultimate ability of an asset-pricing model to explain the equity premium

[^0]thus hinges on successfully identifying an appropriate pricing kernel and accurately modeling corporate cash flows.

Since the equity premium puzzle was identified by Mehra and Prescott (1985), considerable progress has been made in specifying pricing kernels. ${ }^{1}$ In contrast, less attention has been paid to the problem of modeling corporate cash flows within this framework. In fact, many papers in this literature sidestep this issue altogether by simply constraining aggregate dividends to equal aggregate consumption. Important exceptions include Merton (1971) and Santos and Veronesi (2001), who model aggregate corporate cash flows as consumption minus a labor income component. In a series of insightful recent papers, Barberis and Huang (2001) and Menzly et al. ( 2002,2003 ) model the cash flows of individual firms in a way that allows aggregate dividends to differ from aggregate consumption. ${ }^{2}$

Modeling cash flows separately from aggregate consumption is crucial since corporate cash flows have historically been far more volatile and sensitive to economic shocks than has aggregate consumption. For example, corporate earnings have been more than 10 times as volatile as consumption growth during the post-war period. Similarly, while aggregate consumption declined nearly $10 \%$ during the early stages of the Great Depression, aggregate corporate earnings were completely obliterated, falling more than $103 \%$. In addition to being more volatile, corporate cash flows are also highly correlated with aggregate consumption because of their strong procyclical behavior. To provide specifics, during the period 1929-2001 the volatility of earnings growth was $29.5 \%$, while the correlation between per capita real consumption and earning growth was $68.7 \%$.

Intuitively, the reason for the extreme volatility and procyclicality of corporate earnings is that stockholders are residual claimants to corporate cash flows. Thus, the compensation of workers is a senior claim to cash flows. In other words, labor contracts provide workers with some degree of insurance against business cycle risk. These contracts make the fraction of labor income in output (or consumption) countercyclical, while the fraction of earnings in output is procyclical. Gomme and Greenwood (1995) document that these business-cycle-related changes in labor income and earnings can be found in many countries.

This paper extends the literature by modeling aggregate dividends as a small but highly volatile and procyclical component of aggregate consumption. The procyclicality and volatility of dividends directly affect the covariance between the pricing kernel and corporate cash flows and significantly affect equilibrium stock values. To capture the sensitivity of corporate cash flows to both the usual "small" economic shocks as well as to rare catastrophic "large" economic shocks, we extend the representative agent framework to allow aggregate dividends and consumption

[^1]to follow distinct exponential-affine jump-diffusion processes. The ratio of aggregate dividends to consumption, which we designate the "corporate fraction", plays a central role in the model.

From the first-order conditions of the representative agent, we obtain an explicit closed-form expression for the stock price. In turn, this allows us to derive a simple expression for the equity premium in which there are three distinct components. The first is the standard Mehra and Prescott (1985) equity premium proportional to the variance of consumption growth, which we call the consumption-risk premium. The second is proportional to the probability of a jump times the product of the jump sizes in consumption and the stock price. We designate this jump-related component the event-risk premium. The third is proportional to the covariance between the growth rates in consumption and the corporate fraction, and is designated the corporate-risk premium. This three-component model of the equity premium nests many of the previous models in the literature and provides a number of new insights about the determinants of the equity premium.

To illustrate the model's asset-pricing implications, we calibrate the model using parameters that approximate the properties of consumption and the corporate fraction during the past century. A novel feature of our approach is that we calibrate the model using imputed dividends (calculated by applying a payout ratio, which we assume to be constant, to aggregate corporate earnings) rather than using reported dividends. The rationale for this stems from the well-known tendency of firms to artificially smooth their dividends over time, thereby delinking reported dividends from actual corporate cash flows.

We show that the high sensitivity of imputed dividends to economic shocks maps into equity premia many times larger than in the standard framework. For example, using a risk aversion coefficient of five, the three components of the equity premium are $0.36 \%, 0.51 \%$, and $1.39 \%$, respectively, giving a total equity premium of $2.26 \%$. Thus, the equity premium implied by the model is more than six times as large as the standard Mehra and Prescott (1985) equity premium (given by the first component). Similar results hold for a variety of other calibrations.

It is important to recognize, however, that the equity premium implied by the model is less than half as large as historical estimates. Thus, the model clearly does not provide a complete resolution of the equity premium puzzle. ${ }^{3}$ Moreover, the Euler equation for the risk-free bond in our model is the standard one, which means that we inherit Weil's (1989) risk-free rate puzzle. Our results do suggest, however, that combining our approach with other elements such as habit formation (as in Campbell and Cochrane, 1999) or investor heterogeneity in incomplete markets (see the discussion in Constantinides, 2002) could play an important role in the ultimate resolution of asset-pricing puzzles.

[^2]The remainder of this paper is organized as follows. Section 2 presents the assetpricing model. Section 3 solves for the equity premium generated by the model and examines its properties. Section 4 discusses the properties of the corporate fraction. Section 5 describes how the model is calibrated. Section 6 examines the asset-pricing implications of the model. Section 7 summarizes the results and makes concluding remarks.

## 2. The model

We extend the Lucas (1978) and Mehra and Prescott (1985) framework by introducing an explicit model of corporate cash flows. In this model, corporate cash flows represent a small but highly volatile fraction of aggregate consumption. This sensitivity to economic shocks has a number of important asset-pricing implications.

We consider an economy populated by a representative agent who maximizes an expected power utility function of the form

$$
\begin{equation*}
\mathrm{E}_{t}\left[\int_{t}^{\infty} \mathrm{e}^{-\delta(s-t)} \frac{C_{s}^{1-\gamma}}{1-\gamma} \mathrm{d} s\right], \tag{1}
\end{equation*}
$$

where $C_{t}$ represents consumption, $\gamma$ is the coefficient of relative risk aversion, and $\delta$ is the subjective discount rate. The agent has two sources of a nondurable consumption good. First, the agent receives an exogenous endowment $I_{t}$ of the consumption good that constitutes his nonfinancial income. Second, the agent is also initially endowed with one share of a stock that pays dividends $D_{t}$ in the form of the consumption good. The stock is thus a claim to dividends instead of consumption, which in equilibrium is given by the sum of dividends and nonfinancial income, $C_{t}=D_{t}+I_{t}$.

We specify the corporate fraction $F_{t}$ of dividends in consumption exogenously as

$$
\begin{equation*}
F_{t}=\frac{D_{t}}{C_{t}}=\exp \left(-X_{t}\right) \tag{2}
\end{equation*}
$$

where $X_{t}$ follows the square-root jump-diffusion process,

$$
\begin{equation*}
\mathrm{d} X=(\mu-\kappa X) \mathrm{d} t-\eta \sqrt{X} \mathrm{~d} Z_{1}+\xi \mathrm{d} q . \tag{3}
\end{equation*}
$$

Here, $Z_{1}$ is a standard Brownian motion and $q$ is a Poisson process with constant intensity $\lambda$. Provided that $\mu, \kappa$, and $\xi$ are positive, the value of $X_{t}$ is nonnegative. In turn, this ensures that the corporate fraction $F_{t}$ is always between zero and one. This property makes intuitive sense given the interpretation of $F_{t}$ as the proportion of total consumption that comes from dividends. It is easily shown that the expected value of the corporate fraction converges to a steady-state value as $s \rightarrow \infty$ because of the mean-reverting nature of these dynamics.

We next assume that aggregate consumption follows the jump-diffusion process

$$
\begin{equation*}
\frac{\mathrm{d} C}{C}=\alpha \mathrm{d} t+\sigma \sqrt{X} \mathrm{~d} Z_{2}-\psi \mathrm{d} q \tag{4}
\end{equation*}
$$

where $0 \leqslant \psi<1$, and $Z_{2}$ is also a standard Brownian motion. The correlation between the two Brownian motions is $\rho \mathrm{d} t$. By allowing changes in both $X_{t}$ and $C_{t}$ to be
driven by Brownian motions, the model captures the sensitivity of dividends and consumption to small or continuous economic shocks. Furthermore, by allowing $\rho<1$, the model captures the feature that small changes in dividends can be influenced by factors other than those driving consumption. Because both $X_{t}$ and $C_{t}$ are affected by a common Poisson process, however, the model allows for large economic shocks or events (such as the Great Depression) to trigger simultaneous jumps in both dividends and consumption. Finally, note from Eq. (4) that expected consumption growth is constant, implying that consumption growth is not predictable. This follows Hall (1978), Campbell and Cochrane (1999), Chan and Kogan (2002), and many others who assume that consumption growth is not predictable.

From Eq. (2), dividends are given by

$$
\begin{equation*}
D_{t}=C_{t} F_{t}=C_{t} \exp \left(-X_{t}\right) . \tag{5}
\end{equation*}
$$

An application of Ito's Lemma implies the dynamics for the dividend process,

$$
\begin{align*}
\frac{\mathrm{d} D}{D}= & \left(\alpha-\mu+\left(\kappa+\rho \sigma \eta+\eta^{2} / 2\right) X\right) \mathrm{d} t \\
& +\sigma \sqrt{X} \mathrm{~d} Z_{1}+\eta \sqrt{X} \mathrm{~d} Z_{2}+\left((1-\psi) \mathrm{e}^{-\xi}-1\right) \mathrm{d} q \tag{6}
\end{align*}
$$

Comparing these dynamics with those in Eq. (4) shows that dividends have the potential to be more volatile than consumption in this framework because dividend dynamics are driven by both Brownian motions. Similarly, these dynamics allow jumps in dividends to be larger than jumps in consumption. This feature is particularly important since it allows the model to avoid the Mehra and Prescott (1988) critique of the Rietz (1988) model. Rietz argues that the historical equity premium can be explained by the risk of large downward jumps (possibly as large as $90 \%$ ) in consumption. Mehra and Prescott argue that the size of the downward jumps in consumption necessary to explain the equity premium is many times larger than any ever experienced in U.S. history. By allowing us to specify the jump in dividends separately from the jump in consumption, our model is in a better position to capture the historical equity premium without resorting to unrealistically large consumption crashes.

Taken together, these results imply that dividend growth is more sensitive to economic shocks whenever the corporate fraction is stochastic. Only when the corporate fraction is deterministic are dividends and consumption growth equally sensitive to economic shocks. In this case, our model reduces to the standard Mehra and Prescott (1985) framework. To see this, note from Eq. (3) that the corporate fraction is deterministic if and only if $\eta=\xi=0$. Substituting these values into Eq. (6) makes the stochastic components of the dynamics for $D$ identical to those for $C$ in Eq. (4).

In equilibrium, the price of the stock satisfies the Euler equation,

$$
\begin{align*}
P_{t} & =\mathrm{E}_{t}\left[\int_{t}^{\infty} \mathrm{e}^{-\delta(s-t)}\left(\frac{C_{s}}{C_{t}}\right)^{-\gamma} D_{s} \mathrm{~d} s\right] \\
& =\mathrm{E}_{t}\left[\int_{t}^{\infty} \mathrm{e}^{-\delta(s-t)}\left(\frac{C_{s}}{C_{t}}\right)^{-\gamma} C_{s} F_{s} \mathrm{~d} s\right] . \tag{7}
\end{align*}
$$

Using the results in Duffie et al. (2000), the appendix shows that the stock price is given by the following closed-form expression:

$$
\begin{equation*}
P_{t}=C_{t} \int_{t}^{\infty} \mathrm{e}^{-\delta(s-t)} A(t, s) F_{t}^{-B(t, s)} \mathrm{d} s, \tag{8}
\end{equation*}
$$

where

$$
A(t, s)=\exp \left(\int_{t}^{s}-\alpha(1-\gamma)-\mu B(t, u)-\lambda\left((1-\psi)^{1-\gamma} \exp (B(t, u) \xi)-1\right) \mathrm{d} u\right)
$$

and $B(t, s)$ is given by

$$
B(t, s)=\frac{\kappa+\rho \sigma \eta(1-\gamma)+\phi}{\eta^{2}}-\frac{2 \phi}{\eta^{2}\left(1-\theta \mathrm{e}^{-\phi(s-t)}\right)}
$$

and where

$$
\begin{aligned}
& \phi=\sqrt{(\kappa+\rho \eta \sigma(1-\gamma))^{2}-\eta^{2} \sigma^{2} \gamma(\gamma-1)} \\
& \theta=\frac{\eta^{2}+\kappa+\rho \sigma \eta(1-\gamma)-\phi}{\eta^{2}+\kappa+\rho \sigma \eta(1-\gamma)+\phi}
\end{aligned}
$$

From this closed-form solution, it is clear that the stock price is a complex function of consumption, the corporate fraction, and the parameters governing their dynamics. As discussed in the appendix, this solution requires that the term under the square root in the definition of $\phi$ be positive. Given typical parameter values, however, this condition is easily satisfied. ${ }^{4}$

## 3. The equity premium

To explore the implications of the model for the equity premium, it is helpful to first simplify notation slightly. Let $\sigma_{C}$ and $\sigma_{F}$ denote the instantaneous volatility of percentage changes in consumption and the corporate fraction, respectively. More precisely, $\sigma_{C}$ and $\sigma_{F}$ denote the instantaneous volatility of the continuous portion of $\mathrm{d} C / C$ and $\mathrm{d} F / F$, respectively. By a simple extension of the results in Cochrane (2001) to jump-diffusion processes, the appendix shows that the equity premium $E P$

[^3]implied by the model can be expressed as
\[

$$
\begin{equation*}
E P=\gamma \sigma_{C}^{2}-\lambda J_{A} J_{P}+\gamma H \rho \sigma_{C} \sigma_{F}, \tag{9}
\end{equation*}
$$

\]

where $J_{\Lambda}$ is the percentage jump in marginal utility, $J_{P}$ is the percentage jump in the stock price, and $H$ is the elasticity of the stock price with respect to $F$.

This expression illustrates that the equity premium implied by the model has three distinct components. The first term, $\gamma \sigma_{C}^{2}$, corresponds to the equity premium implied by many traditional models; for example, see the recent review paper by Mehra (2002). To make things more clear, we call this first component of the equity premium the consumption-risk premium. As is well known, this first term by itself generates a very small equity premium given the low volatility of historical aggregate consumption data and reasonable levels of the risk aversion coefficient. To provide a simple numerical illustration, assume a value for consumption volatility of $3 \%$ and a value of five for the risk aversion coefficient. From Eq. (9), the value for the consumption-risk premium is then only $0.45 \%$.

The second term is directly related to the effect of a jump on the equilibrium price of the stock. A jump event has two potential effects on the Euler equation defining the price of the stock in that it affects both consumption and the dividend stream. In particular, a downward shock in consumption has the effect of increasing the representative agent's marginal utility. Thus, $J_{\Lambda}$ is positive. On the other hand, the shock to dividends results in a price decline, which means that $J_{P}$ is negative. Thus, the second term $-\lambda J_{\Lambda} J_{P}$ is positive in sign, and can be directly interpreted as the event-risk premium or jump component of the equity premium.

When jumps cannot occur, $\lambda=0$, and the event-risk premium becomes zero. Alternatively, if jumps affect only dividends and not consumption, $J_{A}=0$, and the event-risk premium is again zero. The presence of the event-risk component in the equilibrium equity premium parallels Rietz (1988) in which large downward jumps in consumption affect asset prices. Unlike Rietz, however, our model allows the jump in dividends to differ in size from the jump in consumption. As we show later, this allows the model to generate a large event-risk premium even when the downward jump in consumption is realistic by historical standards. To continue our numerical illustration, assume that a major event such as the Great Depression happens every 100 years on average, resulting in a $10 \%$ decline in consumption and a $75 \%$ decline in the stock market. The corresponding percentage increase in marginal utility $J_{\Lambda}$ is simply $\left(0.9^{-5}-1\right)$, or $69.4 \%$. Thus, the event-risk premium is $0.01 \times 0.694 \times$ $0.750=0.0052$, or $0.52 \%$. This simple example shows that the event-risk premium can be larger than the usual Mehra and Prescott (1985) consumption-risk equity premium given jumps in consumption and the stock market similar to those during the early 1930s.

The third term in the equity premium is directly related to the covariance between consumption growth and percentage changes in the corporate fraction. For example, if dividends are a constant fraction of consumption (as in Mehra and Prescott, 1985), then $\sigma_{F}=0$, which implies that this component of the equity premium is zero. Note that this is true even if the ratio of dividends to consumption is not one. Alternatively, if the correlation $\rho$ between the continuous changes in $C_{t}$ and $F_{t}$ is
zero, then this component is again zero. We designate this third term the corporaterisk premium. To provide a realistic upper bound on how much the corporate-risk premium could potentially contribute to the total equity premium, consider the extreme case where both the correlation and elasticity coefficients are equal to one. Using values for $\sigma_{C}$ and $\sigma_{F}$ of $3 \%$ and $30 \%$, respectively, Eq. (9) implies a value for the corporate volatility premium of $4.50 \%$, which is ten times as large as the consumption volatility premium. Totaling all three of the risk premia in this numerical illustration gives a rough upper bound for the equity premium of $0.45 \%$ $+0.52 \%+4.50 \%=5.47 \%$, which is clearly on the right order of magnitude. In the next several sections, we provide a simple approach for calibrating the model and examining more carefully its implications for the equity premium.

## 4. Measuring the corporate fraction

One of distinguishing features of our framework is that dividends are explicitly modeled as a stochastic fraction of total consumption. Since this corporate fraction plays a key role throughout our framework, we describe how it is estimated and provide summary statistics about its properties.

In theory, the corporate fraction could be estimated by taking reported aggregate dividends and dividing them by aggregate consumption. In actuality, however, there are important reasons why the resulting estimate of the corporate fraction might not be appropriate. Foremost among these is the extensive evidence that corporations tend to artificially smooth dividends over time. Specifically, firms tend to retain earnings during good periods, and to pay dividends out of capital during bad periods. ${ }^{5}$ Clearly, if firms manage their dividends for reasons related to their information or signaling content (e.g. Bhattacharya, 1979; Miller and Rock, 1985), or to resolve agency conflicts (Allen and Michaely, 2002), then the stochastic properties of reported dividends might not be directly linked to the actual cash flows generated by firms. Interestingly, Fama and French (2001) show that firms that do not pay any dividends now account for one-quarter of the value of the stock market. In addition, as argued by Liang and Sharpe (1999), Hall (2001), and others, reported dividends might not include important cash distributions such as share repurchases or corporate acquisitions. Allen and Michaely document that the amount of share repurchases is much more volatile than dividends. ${ }^{6}$ These considerations provide a compelling motivation for using a measure of dividends that more closely reflects actual corporate cash flows.

To this end, we adopt the intuitive approach of assuming that aggregate "economic" dividends are equal to a constant payout ratio times aggregate

[^4]corporate earnings. This approach is used in a number of recent papers such as Lee et al. (1999), Bakshi and Chen (2001), and others. Furthermore, this approach is consistent with the evidence in Lintner (1956), Fama and Babiak (1968), and others that dividend policy is well described by a model in which firms apply a target payout ratio to earnings in making dividend decisions. An important feature of this approach is that percentage changes in imputed dividends are equal to percentage changes in earnings. Thus, the volatility and correlation properties of growth rates in imputed dividends mirror those of corporate earnings.
To provide historical perspective, we collect data on the corporate fraction for the period 1929-2001. The inclusion of the 1930s in the sample is particularly important given the peso-problem-like difficulty in estimating the size and frequency of catastrophic events that could lead to a significant event-risk component in the equity premium. The annual earnings and consumption data used to compute $F_{t}$ are from the National Income and Product Accounts (NIPA) reported by the Bureau of Economic Analysis. As the earnings measure, we use total after-tax corporate profits. We use after-tax rather than pre-tax earnings since dividends are not tax deductible at the corporate level and must be paid out to shareholders on an aftertax basis; see McGrattan and Prescott (2001) for a discussion of the effects of taxes on the equity premium.

Although it could be argued that firms also manage their earnings, there are a number of reasons why out measure of earnings should be largely free of this problem. First, NIPA corporate profit measures are based on Federal tax law rather than on the more flexible rules used by corporations and accounting firms to report financial results to shareholders (typically referred to as GAAP or Generally Accepted Accounting Principles). Second, the NIPA earnings measure excludes many "extraordinary" items, such as capital gains and losses, losses resulting from bad debts, interfirm cash flows, depletion, etc. Finally, since these numbers are aggregated over all firms, any idiosyncratic "extraordinary" items that might cause earnings volatility at the firm level will have less influence on the volatility of aggregate earnings. For example, if a transaction involves one firm reporting an extraordinary gain and another an offsetting extraordinary loss, the aggregate should be largely unaffected. A recent survey by the American Institute of Certified Public Accountants estimates that fewer than $10 \%$ of firms report extraordinary items.

It is important to note that the NIPA measure of earnings does not simply equal total consumption minus labor income. The reason for this is that the National Income accounts also include components such as proprietors' income, rental income, and net interest. Because these components do not accrue to corporate shareholders, however, we exclude them in our measure of earnings since our focus is on valuing equity claims. This is a key distinction between our approach and other papers in the literature that model aggregate dividends as aggregate consumption minus some measure of aggregate labor income. Consumption is defined as the sum of aggregate nondurable and services consumption. In computing real growth rates in consumption, our estimates of realized inflation are based on the price series corresponding to our definition of consumption (not the CPI). Year-end population
estimates used to calculate per capita consumption are from the Census Bureau. Consistent with the historical average for this period, we assume that the payout ratio is $50 \%$. For example, for the period 1929-2001, the median payout ratio is $46.5 \%$, and the average payout ratio (excluding the two years with negative earnings) is $54.6 \%$. In Allen and Michaely (2002, Table 1), the average dividend payout ratio is $45.2 \%$ over the period 1972-1998. Varying the payout ratio has little effect on any of the results, however.

Fig. 1 plots the time series of the corporate fraction for the period 1929-2001. One of the most striking features of the corporate fraction is its volatility. The corporate fraction ranges from a low of $-2.11 \%$ in 1932 to a maximum of $7.81 \%$ in 1959. The average value of the corporate fraction is $4.92 \%$. The standard deviation (in levels) of the corporate fraction is $1.62 \%$, which is $32.99 \%$ of its mean value. This figure closely parallels the $27.03 \%$ standard deviation of percentage changes in the corporate fraction. (Since earnings for 1931-1932 are negative, we compute the percentage changes in the corporate fraction for these years relative to 1930 and then annualize the percentages; this likely results in the volatility of percentage changes being understated.) Another indication of the extreme sensitivity of the corporate fraction to economic shocks is that while consumption declined $8.91 \%$ during the early stages of the Great Depression, the corporate fraction declined $103.35 \%$. The first-order serial correlation of percentage changes in the corporate fraction is 0.058 .

A key feature of the corporate fraction is its surprisingly high correlation with consumption. During the 1929-2001 sample period (excluding 1931 and 1932), the correlation between percentage changes in the corporate fraction and percentage changes in consumption growth is 0.632 , as can be seen in Fig. 2. Clearly, there is a strong positive correlation between the two variables; the $t$-statistic for consumption growth from the regression of percentage changes in the corporate fraction on consumption growth is 6.54 . Thus, the corporate fraction varies significantly with the business cycle; the corporate fraction is highly procyclical. In particular, a $1 \%$


Fig. 1. Time series plot of the corporate fraction for the period 1929-2001. The corporate fraction is the ratio of aggregate after-tax corporate earnings to aggregate consumption times the payout ratio.


Fig. 2. Plot of the corporate fraction growth rate against real consumption growth per capita for the period 1929-2001 (the years 1931-1932 are excluded). The corporate fraction is the ratio of aggregate after-tax corporate earnings to aggregate consumption times the payout ratio.
decline in consumption is associated with roughly a $6 \%$ decline in the corporate fraction. In turn, this implies about a $7 \%$ decline in dividends. The procyclicality of dividends has important implications for the size of the corporate-risk premium.

There are a number of important theoretical and empirical reasons why the corporate fraction should be strongly procyclical. The distribution of income between capital and labor income plays a critical role throughout much of the macroeconomic literature during the past several decades. One of the main components of capital income is corporate profits (the other components are net interest, rental income, and depreciation). As documented by Gomme and Greenwood (1995), the share of income going to capital is highly procyclical in the U.S. as well as in the eight other OECD countries they study. This share approximates the corporate fraction if one thinks of capital income as being mostly corporate profits and of consumption as being roughly equal to income. Gomme and Greenwood show that procyclicality arises naturally in a model where entrepreneurs insure workers against business cycle fluctuations because entrepreneurs (or shareholders) therefore become residual claimants to corporate cash flows.

To provide additional empirical evidence about the procyclicality of the corporate fraction, we investigate a number of alternative approaches for estimating the correlation. For example, using the extensive historical dataset on stock prices, earnings, and consumption collected by Shiller (1989), we calculate the correlation between annual growth rates for real per capita consumption and earnings on the S\&P Composite Stock Price Index for the 1889-1985 period. Although earnings on the S\&P index represent only a small proportion of aggregate corporate profits, the estimated correlation of 0.454 is similar to that based on the NIPA data. Shiller explains that prior to $1926, \mathrm{~S} \& \mathrm{P}$ does not report earnings on the index and that
earnings data for the pre-1926 period are based on average price-earnings ratios. Using only the data for the 1926-1985 period, the correlation estimate is $0.568 .^{7}$

For an alternative measure of the corporate fraction, we collect data from the 2002 Economic Report of the President about aggregate corporate income tax and total income tax revenues for the period 1959-2001. Using the ratio of corporate income tax revenues to total income tax revenues as a proxy for the corporate fraction, the correlation between percentage changes in the corporate fraction and in real per capita consumption is 0.546 . We use a similar approach to estimate the corporate fraction in several other countries for which we could find tax data. Based on data from the Inland Revenue Service of the U.K., the correlation between annual percentage changes in the corporate fraction and real per capita consumption in the U.K. is 0.490 for the period 1978-2002. Similarly, based on data from the Department of Finance for Canada, the correlation between percentage changes in the corporate fraction and real per capita consumption in Canada is 0.436 for the period 1962-2002. Although the ratio of corporate to total income tax revenues is clearly a noisy estimate of the corporate fraction (i.e., it is affected by changes in tax rates, by the progressivity of tax rates, etc.), these high correlations provide independent support for the strong correlation of the corporate fraction and consumption found in the NIPA data. ${ }^{8}$

## 5. Model calibration

In examining the asset-pricing implications of the model, we provide a simple benchmark calibration that captures the historical properties of the data. To gain more insight into these asset-pricing implications, however, we also use a range of realistic alternative values for a number of key model parameters.

First, to hold fixed the properties of the pricing kernel throughout the analysis, the results are all based on a modest level of five for the risk aversion coefficient $\gamma$ of the representative agent. We also assume that the subjective discount rate $\delta$ is 0.01 .

Second, to calibrate the jump-related parameters, we use estimates that reflect the U.S. experience during the Great Depression. In particular, we use a benchmark value for $\lambda$ of 0.01 , implying that a major economic crash occurs every 100 years on average. This mean frequency could actually be overly conservative given the experience of other major economies such as Germany and Japan during the past century. For the consumption jump size $\psi$, we assume a downward jump of $10 \%$. This value is consistent with the $8.9 \%$ downward jump in consumption during 1932, and the $16 \%$ decline from 1929 to $1932 .{ }^{9}$ Next, we assume that the realization of the

[^5]Poisson event in the model results in a $90 \%$ decrease in corporate earnings and imputed dividends. Again, this is on the conservative side given the more than 103\% decline in corporate earnings during the early stages of the Great Depression.

Third, consistent with the properties of consumption during the 1929-2001 period, we assume that the instantaneous mean and standard deviation of consumption growth are $2.34 \%$ and $2.86 \%$, respectively. ${ }^{10}$ Setting these values equal to the instantaneous first and second moments implied by Eq. (4) gives the following simple expressions:

$$
\begin{align*}
& 0.0234=\alpha-\lambda \psi  \tag{10}\\
& 0.0286^{2}=\lambda \psi^{2}-\sigma^{2} \ln \bar{F} \tag{11}
\end{align*}
$$

which are easily solved for $\alpha$ and $\sigma$. Here, the moments are evaluated at the average value $\bar{F}=0.0492$ of the corporate fraction in the sample.

Fourth, the appendix shows that the expected instantaneous change in the corporate fraction is positive for small values of $F$ and negative for large values of $F$. Setting this expected change equal to zero when the corporate fraction equals $\bar{F}$ and using a value of $27.03 \%$ for the instantaneous volatility of the fraction implies the following two expressions:

$$
\begin{align*}
& 0=-\mu-\left(\kappa+\eta^{2} / 2\right) \ln \bar{F}+\lambda\left(\mathrm{e}^{-\xi}-1\right),  \tag{12}\\
& 0.2703^{2}=-\eta^{2} \ln \bar{F}+\lambda\left(\mathrm{e}^{-\xi}-1\right)^{2}, \tag{13}
\end{align*}
$$

which likewise are easily solved for the parameters $\mu$ and $\eta$. For $\kappa$, we use a value of 0.058 , matching the first-order serial correlation coefficient for percentage changes in the corporate fraction during the sample period. Finally, given the properties of the corporate fraction described in the previous section, we use a value of 0.632 for the correlation parameter $\rho$. Table 1 summarizes the calibration assumptions and parameters. ${ }^{11}$

## 6. Asset-pricing implications

Given our benchmark calibration, it is now straightforward to solve for the equity premium and its components. Table 2 reports the values of the equity premium implied by the benchmark calibration. Also reported in Table 2 are values implied by alternative sets of some of the key parameters of this model.

[^6]Table 1
Benchmark calibration values
This table reports the values for the indicated calibration inputs. The parameter estimates are based on NIPA data on annual real per capita consumption and after-tax corporate earnings for the period 19292001. The corporate fraction is the ratio of aggregate after-tax corporate earnings to aggregate consumption times the payout ratio. Consumption is defined as the sum of aggregate nondurable and services consumption. Jump size parameters correspond to the approximate magnitude of the decline in consumption and the corporate fraction during the early stages of the Great Depression. Consumption growth and volatility represent the mean and standard deviation of annual percentage changes in real per capita consumption. Mean corporate fraction is the time-series average of the corporate fraction. Fraction volatility and autocorrelation are the indicated moments for the annual percentage change in the corporate fraction. The correlation coefficient represents the correlation between percentage changes in real per capita consumption growth and in the corporate fraction.

| Calibration input | Value |
| :--- | ---: |
| Risk aversion coefficient | 5.00 |
| Subjective discount rate | 0.01 |
|  |  |
| Probability of a jump | $1.00 \%$ |
| Jump in consumption | $-10.00 \%$ |
| Jump in dividends | $-90.00 \%$ |
|  |  |
| Consumption growth | $2.34 \%$ |
| Consumption volatility | $2.86 \%$ |
|  |  |
| Mean corporate fraction | $4.92 \%$ |
| Fraction volatility | $27.03 \%$ |
| Fraction autocorrelation | $5.80 \%$ |
| Correlation coefficient | $63.20 \%$ |

As shown, the total equity premium is $2.26 \%$ in the benchmark case. This equity premium consists of a $0.36 \%$ consumption-risk premium, a $0.51 \%$ event-risk premium, and a $1.39 \%$ corporate-risk premium. Note that the total equity premium implied by this calibration is more than six times as large as the traditional Mehra and Prescott (1985) equity premium (given by the first or consumption-risk component). Thus, our approach of explicitly modeling corporate cash flows and calibrating the model to earnings data clearly can increase the equilibrium equity premium by nearly an order of magnitude.

Table 2 also shows the sensitivity of the equity premium to some of the key parameters that are unique to this modeling framework. As shown, the mean value of the corporate fraction has only a second-order effect on the equity premium. In contrast, the volatility of changes in the corporate fraction, the correlation coefficient, and the serial correlation coefficient all have large effects on the equity premium. Furthermore, this effect comes predominantly (but not exclusively) through their effects on the corporate-risk component of the equity premium. Finally, an increase in the risk of a large economic shock has the effect of significantly increasing the total equity premium. Note, however, that as the probability of a large jump increases, the volatility of the continuous shocks in $C$ and $F$ must decrease to hold fixed the total volatility of percentage changes in these

## Table 2

Equity premia for varying parameter values
This table reports the value of the three components of the equity premium - consumption risk, event risk, and corporate risk-along with the total equity premium for the indicated parameter values. The first row reports results for the benchmark calibration. For the alternative scenarios, the parameter values differing from the benchmark are listed explicitly; values that are the same as in the benchmark are denoted with a dash.

| Mean value of fraction | Volatility of fraction | Correlation coefficient | Probability of a jump | Serial correlation | Consumption-risk premium | Event-risk premium | Corporate-risk premium | Total equity premium |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4.92\% | 27.03\% | 63.20\% | 1.00\% | 5.80\% | 0.36 | 0.51 | 1.39 | 2.26 |
| 2\% | - | - | - | - | 0.36 | 0.52 | 1.40 | 2.28 |
| 10\% | - | - | - | - | 0.36 | 0.51 | 1.37 | 2.24 |
| - | 20\% | - | - | - | 0.36 | 0.51 | 0.97 | 1.84 |
| - | 50\% | - | - | - | 0.36 | 0.51 | 2.65 | 3.52 |
| - | - | 30\% | - | - | 0.36 | 0.50 | 0.64 | 1.50 |
| - | - | 100\% | - | - | 0.36 | 0.52 | 2.27 | 3.15 |
| - | - | - | 2\% | - | 0.31 | 1.04 | 1.22 | 2.57 |
| - | - | - | 5\% | - | 0.16 | 2.65 | 1.70 | 3.51 |
| - | - | - | - | 2\% | 0.36 | 0.58 | 1.77 | 2.71 |
| - | - | - | - | 10\% | 0.36 | 0.44 | 1.10 | 1.90 |

variables. Thus, both the consumption-risk and corporate-risk premia decrease as the probability of a jump increases.

Although not shown, we also examine the sensitivity of the equilibrium equity premium to a number of the other parameters in the model. These results indicate that the effects of changes in parameters such as the risk aversion coefficient, the volatility of consumption, and the size of the jumps in consumption or the corporate fraction are exactly as implied by the expression for the equity premium in Eq. (9). Not surprisingly, changes in the subjective discount rate and the expected growth rate of consumption have very little effect on the equity premium. Finally, changes in the assumed payout ratio have virtually no effect on the equity premium.

By applying Ito's Lemma to the closed-form solution for the stock price, it is straightforward to solve for the instantaneous volatility of stock returns. Using the parameters for the benchmark scenario gives a stock return volatility measure of $17.37 \%$. This closely approximates the actual volatility of market returns during most of the past century. For example, the annualized volatility of monthly returns on the CRSP value-weighted index for the period 1929-2000 is $19.20 \%$.

Given the closed-form solution for equity values in the model, it is also straightforward to solve for the effect of a catastrophic event or jump on the stock value. Under the benchmark scenario, the stock value declines by $74.15 \%$ when a jump event occurs. While this is clearly much larger than the associated $10 \%$ decline in consumption, it is significantly less than the $90 \%$ decline in dividends. Intuitively, equity values decline less than dividends since the mean reversion in the corporate fraction implies that the effects of a downward jump are not permanent. The $74.15 \%$ value for the benchmark scenario is in close agreement with the historical evidence from the Great Depression. For example, the Dow Jones 30 stock index declined by 69\% during the two-year 1930-1931 period. During 1931 alone, the Dow Jones 30 index fell by $53 \%$.

Although our model is calibrated to U.S. data, our results are also consistent with the experience of many other major countries that have undergone large economic shocks. For example, Jorion and Goetzman (1999) examine stock market returns for countries that experienced shocks severe enough to result in temporary stock market closures. They report the return for the period from just prior to the closure to the date of reopening. Their Table IV reports that Greece experienced a $58 \%$ decline, Japan a $95 \%$ decline, Germany a $84 \%$ decline, and Portugal a $86 \%$ decline during the periods of closures. Of course, there are countries such as China where the economic shocks were so severe that investors presumably lost $100 \%$ of the value of their stockholdings.

## 7. Conclusion

We explore the asset-pricing implications of allowing cash flows to differ from aggregate consumption in a representative agent model with power utility. To model cash flows, we specify processes for consumption and the fraction of dividends in aggregate consumption, which we call the corporate fraction. Consistent with their
historical properties, these processes can be modeled as affine jump-diffusions. We show that equilibrium stock prices can be computed in closed form in this economy.

To measure cash flows, we assume a constant payout ratio and use aggregate data on earnings. The resulting cash flow series is more sensitive to economic shocks, including catastrophic shocks, than are data on aggregate consumption. The series is also highly correlated with consumption growth. These two empirical properties are key features of our calibration.

For calibrated parameter values, we find that our model is able to generate an equity premium that is many times larger than in the standard model. We can write the equity premium in our model as the sum of three components. The first component is the standard consumption-risk premium. This component is small, because consumption growth is smooth. The second component is an event-risk premium due to large catastrophic shocks, such as the Great Depression. Even under conservative assumptions about the probability of a large catastrophic shock and the size of its impact on earnings and consumption, we find that this component is larger than the first. The third component is the corporate-risk premium. Because cash flows are volatile and highly correlated with consumption growth, the third component constitutes the largest portion of the equity premium. We also compute the volatility of equilibrium returns. We find that our model is able to match the return volatility in the data.

## Appendix A

## A.1. Solving for the stock price

Let $Y_{t}$ denote $\ln C_{t}$. Taking the expectation inside the integral in Eq. (7) requires evaluating terms of the form

$$
\begin{equation*}
\mathrm{E}_{t}\left[\exp \left(-X_{s}+(1-\gamma) Y_{s}\right)\right] . \tag{A.1}
\end{equation*}
$$

From Duffie et al. (2000, Proposition 1), these expectations can be expressed in the following form:

$$
\begin{equation*}
A(t, s) \exp \left(B(t, s) X_{t}+C(t, s) Y_{t}\right) \tag{A.2}
\end{equation*}
$$

where $A(t, s), B(t, s)$, and $C(t, s)$ satisfy the system of ordinary differential equations,

$$
\begin{align*}
& \frac{A^{\prime}}{A}=-\alpha C-\mu B-\lambda\left[(1-\psi)^{C} \exp (B \xi)-1\right]  \tag{A.3}\\
& B^{\prime}=\sigma^{2}\left(C-C^{2}\right) / 2+(\kappa+\rho \sigma \eta C) B-\eta^{2} B^{2} / 2,  \tag{A.4}\\
& C^{\prime}=0 \tag{A.5}
\end{align*}
$$

subject to the boundary conditions $A(s, s)=1, B(s, s)=-1$, and $C(s, s)=1-\gamma$. From (A.5), it is immediate that $C(t, s)=1-\gamma$. Substituting this expression for $C(t, s)$ into (A.4) gives a simple Riccati equation for $B(t, s)$ which can be solved by a direct integration. Given typical parameter values, the term under the square root in
the definition of $\phi$ is positive and the solution for $B(t, s)$ is as shown in Eq. (8). When the term under the square root in the definition of $\phi$ is negative, there is a periodic solution for $B(t, s)$ which can become infinite as $s \rightarrow \infty$. With little loss of generality, we abstract from this periodic solution and require the parameter values to be such that $\phi$ is well defined. The term $A(t, s)$ is then given by direct integration once $C(t, s)$ is substituted into (A.5).

With the solutions for $A(t, s), B(t, s)$, and $C(t, s)$, we substitute the expression in (A.2) into Eq. (7). Dividing this expression for the expectation by the $C_{t}^{-\gamma}=$ $\exp \left(-\gamma Y_{t}\right)$ term that appears in the denominator of the agent's marginal utility implies that the solution is linear in $C_{t}$. Recall that $F_{t}=\mathrm{e}^{-X_{t}}$, which implies $\exp \left(B(t, s) X_{t}\right)=F_{t}^{-B(t, s)}$. Substituting this into Eq. (7) gives Eq. (8).

## A.2. The dynamics of the corporate fraction

Recall that $X_{t}=-\ln F_{t}$. Applying Ito's Lemma to $F_{t}=\mathrm{e}^{-X_{t}}$ implies the following dynamics:

$$
\begin{equation*}
\frac{\mathrm{d} F}{F}=\left(-\mu-\left(\kappa+\eta^{2} / 2\right) \ln F\right) \mathrm{d} t+\eta \sqrt{-\ln F} \mathrm{~d} Z_{1}+\left(\mathrm{e}^{-\xi}-1\right) \mathrm{d} q . \tag{A.6}
\end{equation*}
$$

Since $X_{t}$ is nonnegative, $F_{t}$ takes values between zero and one. It is also easily shown that $F_{t}$ has a stationary long-run mean value (by solving for the value of $E_{t}\left[\mathrm{e}^{-X_{s}}\right]$ and taking the limit as $s \rightarrow \infty$ ). That $F_{t}$ displays mean-reverting behavior is also clear from its dynamics. In particular, since $\ln F_{t}<0$, the drift term in (A.6) is positive for values of $F_{t}$ close to zero, and is negative for values of $F_{t}$ close to one. Taking expectations in (A.6) implies

$$
\begin{equation*}
\mathrm{E}_{t}\left[\frac{\mathrm{~d} F}{F}\right]=\left(-\mu-\left(\kappa+\eta^{2} / 2\right) \ln F\right) \mathrm{d} t+\lambda\left(\mathrm{e}^{-\xi-1}\right) \mathrm{d} t \tag{A.7}
\end{equation*}
$$

Setting the left-hand side of (A.7) equal to zero and evaluating at $F=\bar{F}$ gives Eq. (12). Similarly,

$$
\begin{equation*}
\operatorname{Var}_{t}\left[\frac{\mathrm{~d} F}{F}\right]=-\eta^{2} \ln F \mathrm{~d} t+\lambda\left(\mathrm{e}^{-\xi}-1\right)^{2} \mathrm{~d} t \tag{A.8}
\end{equation*}
$$

which implies Eq. (13) when evaluated at $F=\bar{F}$.

## A.3. The equity premium

Following Cochrane (2001), let $\Lambda_{t}$ denote the stochastic discount factor $\mathrm{e}^{-\delta t} C_{t}^{-\gamma}$ and $P_{t}$ the price of the stock. Using the generalized form of Ito's Lemma to allow for jumps, Cochrane Eq. (1.32) can be expressed as follows:

$$
\begin{equation*}
\mathrm{d}(\Lambda P)=P \mathrm{~d} \Lambda^{*}+\Lambda \mathrm{d} P^{*}+\mathrm{d} P^{*} \mathrm{~d} \Lambda^{*}+\left[\Lambda^{+} P^{+}-\Lambda P\right] \mathrm{d} q \tag{A.9}
\end{equation*}
$$

where changes in the processes superscripted with an asterisk denote continuous changes, and $\Lambda^{+}$and $P^{+}$denote the values of these processes immediately after a
jump. Using this expression, Cochrane Eq. (1.33) becomes

$$
\begin{equation*}
0=\frac{D}{P} \mathrm{~d} t+\mathrm{E}_{t}\left[\frac{\mathrm{~d} \Lambda^{*}}{\Lambda}+\frac{\mathrm{d} P^{*}}{P}+\frac{\mathrm{d} P^{*}}{P} \frac{\mathrm{~d} \Lambda^{*}}{\Lambda}\right]+\lambda\left[\frac{\Lambda^{+} P^{+}}{\Lambda P}-1\right] \mathrm{d} t . \tag{A.10}
\end{equation*}
$$

Using the following expressions,

$$
\begin{align*}
& \frac{\mathrm{d} P}{P}=\frac{\mathrm{d} P^{*}}{P}+\left[\frac{P^{+}}{P}-1\right] \mathrm{d} q  \tag{A.11}\\
& \frac{\mathrm{~d} \Lambda}{\Lambda}=\frac{\mathrm{d} \Lambda^{*}}{\Lambda}+\left[\frac{\Lambda^{+}}{\Lambda}-1\right] \mathrm{d} q \tag{A.12}
\end{align*}
$$

to substitute out terms in (A.10) gives

$$
\begin{align*}
0= & \frac{D}{P} \mathrm{~d} t+\mathrm{E}_{t}\left[\frac{\mathrm{~d} \Lambda}{\Lambda}\right]+\mathrm{E}_{t}\left[\frac{\mathrm{~d} P}{P}\right] \\
& +\mathrm{E}_{t}\left[\frac{\mathrm{~d} P^{*}}{P} \frac{\mathrm{~d} \Lambda^{*}}{\Lambda}\right]+\lambda\left[\frac{\Lambda^{+} P^{+}}{\Lambda P}-\frac{P^{+}}{P}-\frac{\Lambda^{+}}{\Lambda}+1\right] \mathrm{d} t . \tag{A.13}
\end{align*}
$$

Rearranging terms and using Eq. (1.34) of Cochrane gives

$$
\begin{equation*}
E P \mathrm{~d} t=-\mathrm{E}_{t}\left[\frac{\mathrm{~d} P^{*}}{P} \frac{\mathrm{~d} \Lambda^{*}}{\Lambda}\right]-\lambda\left(\frac{\Lambda^{+}}{\Lambda}-1\right)\left(\frac{P^{+}}{P}-1\right) \mathrm{d} t . \tag{A.14}
\end{equation*}
$$

An application of Ito's Lemma implies

$$
\begin{align*}
\frac{\mathrm{d} P^{*}}{P} & =(\cdot) \mathrm{d} t+\left(\frac{\mathrm{d} C^{*}}{C}\right)+\left(\frac{F P_{F}}{P}\right)\left(\frac{\mathrm{d} F^{*}}{F}\right),  \tag{A.15}\\
\frac{\mathrm{d} \Lambda^{*}}{\Lambda} & =(\cdot) \mathrm{d} t-\gamma\left(\frac{\mathrm{d} C^{*}}{C}\right) \tag{A.16}
\end{align*}
$$

Substituting into (A.14), taking expectations, and using the notation introduced in the text now gives Eq. (9).

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[^1]:    ${ }^{1}$ Important recent examples include Eichenbaum et al. (1988), Sundaresan (1989), Constantinides (1990), Abel (1990), Epstein and Zin (1991), Ferson and Constantinides (1991), Detemple and Zapatero (1991), Heaton (1995), Chapman (1998), Campbell and Cochrane (1999), Hansen et al. (1999), Lettau and Uhlig (2000), Wachter (2003), Chen and Epstein (2002), among many others.
    ${ }^{2}$ Other important papers that allow aggregate cash flows to differ from aggregate consumption include Campbell (1986), Cecchetti et al. (1993), Campbell and Cochrane (1999), Abel (1999), Bekaert and Grenadier (1999), Brennan and Xia (2001), and others.

[^2]:    ${ }^{3}$ There is an extensive literature on the equity premium puzzle. Detailed references can be found in the excellent surveys by Kocherlakota (1996), Cochrane (1997), Campbell (1999), Constantinides (2002), and Mehra (2002). Breeden (1979) and Bakshi and Chen $(1996,1997)$ are continuous-time versions of the endowment economy in Lucas (1978) based on diffusions. Naik and Lee (1990) extend the setup to allow for jumps in consumption growth. Their model is the continuous-time analogue of Rietz (1988).

[^3]:    ${ }^{4}$ Other recent papers that provide solutions for equity prices in terms of their fundamental cash flows include Ohlson (1990, 1995), Bakshi and Chen (1996, 1997, 2001), Bekaert and Grenadier (1999), Ang and Liu (2001), Vuolteenaho (2002), Mamaysky (2002), and Pastor and Veronesi (2003).

[^4]:    ${ }^{5}$ Evidence on this tendency dates back as far as Lintner (1956), Brittain (1966), and Fama and Babiak (1968). More recent examples documenting this tendency include Marsh and Merton (1987), DeAngelo et al. (1992), Allen and Michaely (2002), and many others.
    ${ }^{6}$ For an analysis of the tradeoffs between paying dividends and repurchasing shares, see Chowdhry and Nanda (1994) and Allen et al. (2000).

[^5]:    ${ }^{7}$ The correlation for the 1889 to 1985 period excludes the crash of 1921-1922 since this represents a large jump event.
    ${ }^{8}$ We also found data sources from the Ministry of Finance for Japan in which a measure of aggregate pre-tax corporate profits is reported. Using this to calculate the corporate fraction, the correlation between the corporate fraction and consumption is 0.284 for the 1960-2001 period.
    ${ }^{9}$ While downward jumps in consumption of this magnitude are large, there are many examples of economies that have experienced downward jumps in consumption of as much as $20-30 \%$ during the past

[^6]:    (footnote continued)
    50 years. In particular, countries that have experienced a one-year decline in real GDP of more than $20 \%$ since 1950 include Algeria, Angola, Chad, Iran, Iraq, Namibia, Nicaragua, Niger, Nigeria, Sierra Leone, and Uganda (see Heston and Summers, 1991).
    ${ }^{10}$ Campbell (1999, Table 3) reports that the mean and standard deviation of consumption growth during the $1891-1995$ period are $1.77 \%$ and $3.26 \%$, respectively.
    ${ }^{11}$ The standard deviation of earnings growth rates during the $1929-2001$ sample period is $29.5 \%$. The correlation of per capita real consumption and earnings growth rates during the same period (excluding 1931 and 1932) is $68.7 \%$.

