Information Aversion *

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June 27, 2015

Abstract

We propose a theory of inattention solely based on preferences, absent cognitive limitations or external costs of information. Under disappointment aversion, agents are intrinsically information averse. In a consumption-savings problem, we study how information averse agents cope with their fear of information, to make better decisions: they acquire information at infrequent intervals only, and inattention increases when volatility is high, consistent with the empirical evidence. Adding state-dependent alerts following sharp downturns improves welfare, despite the additional endogenous information costs. Our framework accommodates a broad range of applications, suggesting our approach can explain many observed features of decision under uncertainty.

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1 Introduction

Experiencing the roller coaster of life can be stressful. A natural way to avoid this stress is to close your eyes for the ride. We propose a theory of inattention building on this idea. Our unique assumption is a recursive implementation of disappointment aversion (Gul, 1991), a common model of risk attitude. These preferences imply information aversion, a fear of information flows: disappointment averse agents optimally decide to stay away from some sources of information. Our framework has rich implications reflecting key observations on information and risk-taking behavior in the lab and in the field, in particular among financial markets participants. As such, our approach provides a parsimonious, tractable, and empirically appealing preference-based model of inattention.

Our analysis is constructed around three questions. First, we characterize formally the utility costs of receiving signals in settings where information is not instrumental, as documented in the experimental literature. Second, we study how information averse agents cope with their fear of information flows in order to make better decisions. To understand the interaction between information and allocation decisions, we study a problem of consumption and risky savings, where the agent can choose, at any time, to close her eyes and not observe information around her. Finally, we look for better ways to tailor the information received by an information averse agent.

Under disappointment aversion, agents inflate the probabilities of outcomes that disappoint, i.e. fall below an endogenous reference point which reflects their current expectations about the future. As information arrives, each piece of news creates scope for disappointment. The agent therefore prefers to receive less fragmented information and observe simultaneous bundles of news in which good news can cancel out bad, disappointing, news. Such information aversion is a direct consequence of her attitude towards risk.\(^1\) As an illustration, consider an investor owning a stock she has decided to sell exactly a year from now. The investor has a lot of control over the information structure she faces. She can choose to follow the price of the stock

\(^1\)Dillenberger (2010) provides a general characterization of the link between attitude towards risk and attitude towards information.
at different frequencies: continuously, daily, monthly or not at all until the end of the year. Observing intermediate signals is of no direct use to her as she will hold on to the asset anyways. Under expected utility, she would be indifferent between those information structures. A disappointment averse investor, however, unambiguously opts not to observe the price at all over the year. This behavior is widely supported by a number of empirical and experimental findings. Starting with Gneezy and Potters (1997) and Thaler et al. (1997), experiments have consistently showed that subjects’ valuations of risky outcomes diminish when they are given more frequent and more detailed information. Galai and Sade (2006) find similar results using field data on Israeli treasury bills and commercial banks deposits.\(^2\)

Our first contribution is to characterize the magnitudes and properties of the endogenous costs of information implied by disappointment aversion. Information aversion differs fundamentally from both exogenous information costs and cognitive constraints. With one signal, more information is not always more costly; Blackwell ordering is not respected. We analyze how the frequency of information observations impacts the valuation of risky lotteries, whose payoffs are determined by the final outcome of a stochastic process growing with i.i.d. increments, as is natural to assume for an asset price for instance. We derive a useful representation of these valuations as a certainty equivalent rate of return depending of the observation frequency, generalizing the standard notion. The certainty equivalent rate of returns decreases with the frequency of observation (Section 3.2). The magnitude of this effect, however, varies greatly across characteristics of the process. As the frequency of observation increases, a disappointment averse agent is extremely averse to frequent small news, as in a diffusion process, but much less so to infrequent large news, as in a jump process.

Second, we analyze how information averse agents balance the endogenous utility cost of paying attention to the economic environment with the benefits of making better informed decisions. We study the interaction of risk-taking and information decisions through the lens of a standard consumption and savings problem. Going

\(^2\)See also for example, the experiments of Benartzi and Thaler (1999), Barron and Erev (2003), Gneezy et al. (2003), Bellemare et al. (2005), Haigh and List (2005), Fellner and Sutter (2009) and Anagol and Gamble (2011). While some of these were designed to test myopic loss aversion, their results are also consistent with our dynamic disappointment aversion model.
back to our illustrative example, assume now our investor manages her wealth in order to finance her consumption over time, and let her allocate her savings between a risk-free asset, and a risky asset yielding higher average returns. We show she optimally decides to observe the value of her risky portfolio at equally spaced discrete points in time (Proposition 4). In between observations, she consumes deterministically from a risk-less portfolio, and allocates the rest of her wealth to the risky asset. The marginal cost of infrequent observation is due to the loss in expected returns when more wealth is placed in the risk-free asset, captured by the spread between the certainty equivalent rate of the risky asset and the risk-free rate, like in the classic models of Baumol (1952) and Tobin (1956). Novel to their frameworks, and specific to our approach, the marginal benefit comes from a relief from the stress of receiving information, formally represented by the sensitivity of the certainty equivalent rate to the observation interval.

This simple characterization helps understand conditions propice to inattention. Through the fundamental link between information aversion and risk aversion in our model, more risk averse investors are also more inattentive as documented in Alvarez et al. (2012). Periods of high volatility also correspond to more inattention, even when higher expected returns keep the difference between risk adjusted returns and the risk-free rate constant. This prediction reflects an increase in the marginal cost of information as risk increases and is in line with recent empirical evidence: Sicherman et al. (2014) document investors reduce the monitoring of their portfolios when stock market volatility increases. We further show the interplay of attention and risk-taking is far from straightforward: when the agent receives more information, risk-taking can either decrease or increase. Echoing the basic mechanism of information aversion, if information increases to the point the agent no longer values the risky asset above the risk-free one, she exits the risky market, and risk taking decreases to zero. However, as long as information is infrequent enough that the risky asset remains attractive relative to the risk-free asset, another important force is present. If the investor receives more information, even though it is painful and lowers her valuation of the risky asset, she can nonetheless take advantage of this knowledge of the evolution of the risky asset to shift her savings away from the risk-free asset and towards the risky asset. This second force shows the observation of Beshears et al.
(2012), who document in a field experiment that investors do not reduce their risk-taking when receiving more information, does not provide a rebuttal for information aversion.

Third, we ask whether, with the help of a third party, better flow of informations can be obtained than the simple time-dependent rules our investor rules can do alone. Observe our framework allows us to consider arbitrary information structures, since the information costs are completely endogenous. In contrast to Abel et al. (2013), we find state-dependent rules do help. In particular, we show providing “distress” signals following sharp market downturns increases welfare. Such a result echoes the fact extreme bad outcomes take a pregnant place in media, but also suggest financial institutions can foster more investment by providing such signals. We can go further and analyze whether delegating actions can avoid all information costs. In our basic setting, the agent’s optimal consumption reveals information on her wealth, and delegation can only go so far. However, in settings where some decisions only have a long-term impact, delegation is a powerful tool to escape information costs.

Together, these results show a simple and parsimonious assumption for preferences, disappointment aversion, leads to a rich theory of inattention. Not only does our framework provide a joint explanation for behavior observed in the lab and in the field, but also points out novel implications, distinct from the standard applied models on the topic. More than a simple alternative to theories based on exogenous information costs, on the positive side, our approach implies fundamentally different normative consequences. When information costs are due to technological limitations, finding ways to provide more information improves welfare. In contrast, such policies are not always desirable in our setting. More generally, we show opaqueness might be a positive feature of many economic activities.

After a review of the related literature, Section 2 introduces our recursive implementation of disappointment aversion and characterizes the resulting information aversion. Section 3 derives the notion of certainty equivalent rate in a setting where information is not instrumental, and shows how it depends on the information environment. Section 4 analyzes the consumption and savings problem, and the interaction between risk-taking and information decisions. Section 5 considers richer information structures as well as the potential for delegation. Section 6 briefly out-
lines applications of the model to other dimensions of risky decisions with endogenous information choices: leverage, diversification, learning, and agency issues. All mathematical proofs are in the online Appendix.³

Related literature

Under disappointment aversion, “bad” outcomes are overweighted relative to positive ones. This model of preferences incorporates loss aversion, one of the main components of the seminal prospect theory of Kahneman and Tversky (1979). In addition to the large body of work providing direct support to loss aversion, disappointment aversion has proven useful in understanding risk-taking in financial markets.⁴ However, the literature, so far, fails to account for disappointment aversion’s implications for information choices, our focus. Indeed, while Benartzi and Thaler (1995) point out the frequency of utility evaluation matters under loss aversion, they determine this frequency as the result of another behavioral trait: myopia. In contrast, in our setup, this frequency is a choice of the agent. It results from trading off the utility cost of a more frequent information flow with the benefits of better informed decision-making. Our paper provides a framework to formally analyze simultaneously endogenous information and risk-taking decisions with a single assumption about preferences.

Caplin and Leahy (2001, 2004), who relate inattention to anticipatory feelings, as well as the optimal expectations model of Brunnermeier and Parker (2005), also propose preferences in which information can have intrinsic costs. Closer to our analysis, Pagel (2014), in a contemporaneous paper, considers a consumption-savings problem under the news-utility theory of Kőszegi and Rabin (2009), who explicitly model flows of information as costly in the utility function, with time inconsistent dynamics.⁵ Rather than aim at arbitrary information preferences, our approach is more parsimonious: risk aversion implicitly results in information aversion, and both derive from the same unique parameter. Further, the aforementioned preferences, including

³https://sites.google.com/site/marianneandries/IAappendix.pdf
⁴Disappointment aversion can explain portfolio choices (Ang et al., 2005), equilibrium aggregate prices (Routledge and Zin (2010), Bonomo et al. (2011)), and the cross-section of expected returns (Ang et al. (2006), Lettau et al. (2013)).
⁵Hsiaw (2013) considers reference point goal setting as a solution to time inconsistency, with implications for optimal stopping times.
loss aversion as in Kőszegi and Rabin (2009), do not cause an unambiguous dislike for information: signals may be perceived as a benefit, whereas they always come at a utility cost under disappointment aversion (see Proposition 1). Disappointment aversion preferences also have the appeal over standard loss aversion to be axiomatically funded. They have been broadly, and successfully, implemented in the finance literature. Our model is dynamically time consistent and the relative simplicity of our framework allows for a formal analysis of the implicit information costs, and can be readily applied to other optimal decisions problems.

We contribute to the literature on the optimal inattentive behavior of consumers or firms by introducing endogenous observation costs that derive from agents’ preferences for risk. Our preference-based framework provides an alternative to the two main approaches in this literature: cognitive limitations represented by entropy constraints, and exogenous fixed costs of information.

Our endogenous cost structure differs from that implied by the entropy constraints of rational inattention, developed by Sims (1998) and Sims (2006). Intuitively, more than the quantity of information, the structure of the flow of information is the source of cost in our setting, which makes it particularly well suited for analyzing the observed discreteness of information acquisition. Discreteness only arises in particular situations under rational inattention whereas it is a generic feature of our model.6

Closer to our analysis is the literature using exogenous fixed costs of observation, which also imply optimal observation at discrete points in time. Duffie and Sun (1990) solve a portfolio problem similar to ours, assuming observations and transactions must be synchronized, and come at a fixed cost. Abel et al. (2007) derive optimal inattention periods and portfolio decisions under exogenous monetary costs of information. Abel et al. (2013) add transaction costs, Alvarez et al. (2012) durable consumption. Gabaix and Laibson (2002) show slow portfolio readjustment, as a result of inattention, can have a profound impact on equilibrium asset prices.7 In those models, the benefit of information is similar to our setting’s and therefore optimal policies exhibit some similarities. However, our endogenous information costs yield additional

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6Matejka and Sims (2010) provides a characterization of these situations in the context of a tracking problem and Matějka (2010) is an application to a price-setting problem.

7Lynch (1996) also studies the equilibrium implications of infrequent transactions, without an explicit motivation by inattention.
insights on the determination of attention policies, and how attention varies with the environment. Further, our preference-based approach makes possible the comparison of richer information structures, without introducing ad-hoc assumptions about the different costs. At a deeper level, technological or cognitive limitations to information acquisition differ fundamentally from our model, where agents desire to stay away from information. From a normative point of view, our approach shifts the emphasis from a view where facilitating information acquisition is key, to one where helping agents stay away from information or, in a more subtle way, where shaping the information flows they receive are useful policies.

2 Disappointment aversion and information aversion

We introduce the preferences we use along the paper, a recursive implementation of the disappointment aversion model. Our choice of preferences is strongly supported by the recent macro and finance literature, in which they have been utilized to explain both portfolio choices and asset prices. We detail how these preferences result in an unambiguous aversion to information flows, the basic force of our model of inattention.

2.1 Dynamic disappointment aversion

Under loss aversion, one of the main components of the seminal prospect theory model of Kahneman and Tversky (1979), agents value outcomes relative to a reference point, and losses relative to the reference point create more disutility than comparable gains. Disappointment aversion, introduced by Gul (1991), provides a fully axiomatized model of preferences in which agents display such a micro-founded attitude towards risk. For the sake of simplicity, we focus on a piecewise linear spec-

8See, among others, Ang et al. (2005), Routledge and Zin (2010), Bonomo et al. (2011), Ang et al. (2006), Lettau et al. (2013).
For a static lottery with payoff distributed according to \( F \), the certainty equivalent \( \mu_\theta(F) \) is given by

\[
\mu_\theta(F) = \frac{\int x dF(x) + \theta \int_{x \leq \mu_\theta(F)} x dF(x)}{1 + \theta \int_{x \leq \mu_\theta(F)} dF(x)},
\]

where \( \theta \geq 0 \) is the coefficient of disappointment aversion.\(^9\) \( \mu_\theta(F) \) is a weighted average of the potential payoffs, where disappointing payoffs receive a higher weight by a factor \((1 + \theta)\). What defines a payoff as disappointing is whether or not it is below the reference point, or “fair value”, the certainty equivalent itself: equation (1) is a fixed point problem in the certainty equivalent \( \mu_\theta(F) \) (which always admits a unique solution). In this simple specification, the only source of risk aversion comes from the kink at the reference point, and the concavity it entails.

We are interested in the effect of the information flow on the valuation of risky outcomes. To consider this question, we extend these preferences to a dynamic setting. For now, we add intermediate signals; we include intermediate consumption in Section 4. Consistent with the framework of Epstein and Zin (1989) and Weil (1989), and the axiomatization of Kreps and Porteus (1978), we assume a recursive, and time-consistent, dynamic implementation of disappointment aversion. Given certainty equivalent continuation values \( \mu_\theta(s_{t+1}) \) in each possible state \( s_{t+1} \) at date \( t+1 \) and transition c.d.f \( F(s_{t+1}|s_t) \), the certainty equivalent for state \( s_t \) at date \( t \) is given by

\[
\mu_\theta(s_t) = \frac{\int \mu_\theta(s_{t+1}) dF(s_{t+1}|s_t) + \theta \int_{\mu_\theta(s_{t+1}) \leq \mu_\theta(s_t)} \mu_\theta(s_{t+1}) dF(s_{t+1}|s_t)}{1 + \theta \int_{\mu_\theta(s_{t+1}) \leq \mu_\theta(s_t)} dF(s_{t+1}|s_t)}.
\]

What are the stages \( t, t+1, \ldots \)? Each step of the recursion corresponds to a potential arrival of news. The instant before a piece of information is revealed, our agent fears receiving disappointing news, and adjust downwards her valuation of the lottery accordingly. While in all generality, the timing of information arrival need not coin-

\(^9\)The link with information aversion is robust to adding strict concavity on both sides of the reference point as in the more general case of Gul (1991).

\(^{10}\)We always assume \( \theta \geq 0 \), even though Gul (1991)'s framework allows for negative \( \theta \), i.e. risk seeking.
cide with clock time, we assume they do in most of our applications, as is implicitly
assumed in most standard applied models.

If one considers the certainty equivalent of Equation (2) as a form of distorted
expectation, the corresponding law of iterated expectations is violated. Given the total
information revealed, the composition of when the agent observes the information
affects the valuation of risky payoffs. Our modeling choice for a recursive dynamic
implementation thus determines attitudes towards information. We analyze how in
the next section.

2.2 Attitudes towards information

To clarify attitudes towards information, we analyze the valuation of a final random
payoff $X$, with distribution $F$, under two different information plans. In the first, no
information is received until the payoff is realized, and the ex-ante valuation is $\mu_\theta(F)$
as in Equation (1). In the second, the agent receives an intermediate signal $i \in \mathcal{I}$,
with distribution $\alpha$, and updates her belief on the distribution of $X$, from $F$ to $F_i$. We
note her ex-ante valuation under this information plan, derived from Equation (2),
$\mu_\theta(\{F_i, \alpha(i)\})$.

For expected utility agents, the valuations under the two information plans, $F$ and
$\{F_i, \alpha(i)\}$, are strictly equal. This equality, however, typically does not obtain for more
general preference specifications. Dillenberger (2010) characterizes an equivalence
between a static property of preferences, negative certainty independence, and the
preference for information plans without intermediate information.\footnote{Cerreia-Vioglio et al. (2014) provides a general representation of preferences satisfying negative certainty independence together with additional axioms, cautious expected utility. Their results provides a framework for potential extensions of our analysis to other models of preferences.} Our dynamic
disappointment aversion model satisfies negative certainty independence and therefore
implies an unambiguous aversion to receiving the intermediate signals. From
Dillenberger (2010), we obtain the following proposition:

**Proposition 1.** An agent with dynamic disappointment, as specified in Equation 2,
prefers not to observe intermediate signals:

\[ \forall F, \{ F_i, \alpha (i) \}_{i \in I} \text{ s.t. } F = \int_{i \in I} F_i d\alpha (i), \]

\[ \mu_\theta (\{ F_i, \alpha (i) \}) \leq \mu_\theta (F). \]

We call information aversion this dislike for receiving intermediate information.\(^{12}\)

Information aversion is generic: for most cases of partial information, agents strictly prefer not to receive the signal. The following corollary characterizes the particular cases for which there is indifference.

**Corollary 1.** Agents are indifferent to receiving intermediate information, \( \mu_\theta (\{ F_i, \alpha (i) \}) = \mu_\theta (F) \), if and only if

\[ \forall i, \begin{cases} \mu_\theta (F_i) = \mu_\theta (F) \text{ or } \\ F_i \text{ is degenerate} \end{cases} \]

Receiving intermediate information is costless if and only if each potential signal either fully reveals the final payoff (the intermediate signal is degenerate), or it leaves the valuation for the risky payoff unchanged (e.g. no information, \( F = F_i \)). Our model of preferences thus results in endogenous information costs that obey a “hump-shaped” type structure, where no information or full information have zero costs, but partial information has a strict positive cost.\(^{13}\)

A useful insight from this corollary is that neither the standard informativeness constraints nor the exogenous information costs typically used in the inattention literature can quantify the endogenous information costs in our framework.

**Corollary 2.** For any level of mutual entropy, there exist intermediate signals information plans with that level of mutual entropy and the same valuation \( \mu_\theta (F) \) as the one-shot lottery.

\(^{12}\)Myopic loss aversion, as in Benartzi and Thaler (1995), or the news-utility theory of Kőszegi and Rabin (2009), can appear similar to information aversion. Note, however, the unambiguous dislike for information of Proposition 1 is not satisfied under those models.

\(^{13}\)Observe this distinguishes information aversion from preferences for a late resolution of uncertainty. For instance, in our framework, a fully revealing early signal is preferred to a partial late signal.
Corollary 3. Information costs under our model of preferences are not monotone in Blackwell ordering.

It is thus worthwhile exploring, under our information aversion framework, both the valuation of risk and the link between information and risk-taking decisions.

3 Attention and the cost of information

Starting with Gneezy and Potters (1997) and Thaler et al. (1997), experiments going beyond two-stage lotteries have consistently showed subjects’ valuations of risky outcomes diminish when they are given more frequent and more detailed information, absent any exogenous costs of information. This finding is hard to reconcile with the standard information literature. In this section, we analyze how the frequency of information observation as well as the distribution of the lottery’s payoffs affect its valuation when agents are information averse as in our model of preferences. This analysis provides a theoretical justification for the aforementioned experimental evidence as well as additional predictions on the structure of information costs in our approach.

3.1 The certainty equivalent rate

To fully isolate the costs of information in our framework, and stay close to the experimental evidence, we consider a lottery that cannot be affected by any intermediate decision of the agent. We determine the valuation, at date $t = 0$ of a lottery with payoffs at date $t = \tau$, determined by the time $\tau$ value of an exogenous stochastic process $X = \{X_t\}_{t \in [0, \infty]}$, with i.i.d. growth.\footnote{We focus on a framework with geometric growth, as is standard for asset prices. Most of our results have straightforward equivalents for the case of arithmetic growth.} We assume the process $X$ has an instantaneous expected growth rate $g$, and finite quadratic variation. The agent observes $X_t$ at regular intervals of length $T$. We analyze how the valuation of the lottery depends on this observation interval.

This thought experiment is not only in the spirit of the lab experiments mentioned above, but it also echoes many real-life situations. For instance, one can think of an
investor owning a stock and deciding how often to check its price before selling it, of
the manager of an R&D project deciding on how often to monitor her employees, or of
an individual deciding how often to check the evolution of her health using medical
testing. For all those situations, while the potential benefits of being attentive are
clear, substantial evidence of inattention is present.\textsuperscript{15} This section assumes away
potential benefits and characterizes the cost of attention arising from information
aversion. We consider the tradeoff with benefits in Section 4.

For a risk-neutral agent, the value at time \( t = 0 \) of the lottery with payoff \( X_\tau \) is
\( V_0(\tau) = X_0 \exp(g \tau) \), independent of the observation interval \( T \). Under expected utility,
a simple application of the law of iterated expectations proves the certainty equivalent
does not depend on the observation interval either. In contrast, under our model
of preferences, we show the frequency of observation does matter. Taking advantage
of the fact the certainty equivalent is homogenous of degree 1, and growth is i.i.d., we
can separate the distinct roles of the observation interval and of the horizon.\textsuperscript{16}

\[
V_0(\tau, T) = X_0 \exp(v(T) \tau),
\]
\[
\text{where } \exp(v(T)T) = \mu_\theta \left( \frac{X_T}{X_0} \right).
\]

We define \( v(T) \) as the\textit{ certainty equivalent rate}, which encodes the role of the ob-
servation interval. It corresponds to the risk adjusted rate of return, standard to the
finance literature, and takes into account the valuation of the lottery depends on the
frequency of observation, when agents are information averse. \( v(T) \) is the sum of two
element: the expected growth rate \( g \), and a risk adjustment that depends on the in-
formation flow, is always negative due to risk aversion, and is independent of \( g \); we
focus on this component by analyzing martingale processes hereafter. The following
proposition gathers some general properties of the certainty equivalent rate.

\textbf{Proposition 2.} For information averse agents, the certainty equivalent rate \( v(T) \) ver-
ifies the following properties

\begin{itemize}
  \item \( -Tv(T) \) is subadditive
\end{itemize}

\textsuperscript{15}For instance, Oster et al. (2013) provides evidence in the context of testing for Huntington disease.
\textsuperscript{16}For instance, with two observations, we have: \( V_0(2T, T) = X_0 \mu_\theta(X_T/X_0) \mu_\theta(X_{2T}/X_T) = X_0(\mu_\theta(X_T/X_0))^2 \).
• \( \lim_{T \to \infty} v(T) = g \)

• \( \lim_{T \to 0} T v(T) = 0 \)

• \( v(T) \) is decreasing in the disappointment aversion \( \theta \) for all \( T \)

These properties inform us on the structure of information costs. In the language of cost functions (see e.g. Tirole (1988)), \(-v(T)\) is an average cost function, \(-T v(T)\) being the cost function. The subadditivity of information costs results from information aversion, and provides a justification for the experimental evidence: given a time horizon \( \tau \), the agent always prefers to observe a unique signal rather than to split the information over time. The first limit property shows the average cost of information vanishes as the observation interval becomes large. The second limit property shows information costs disappear altogether when the lottery becomes short-lived, as there is no more information to be had. Finally, at all frequencies, information costs increase with the agent’s information aversion, as represented by \( \theta \).

To further analyze the properties of the certainty equivalent, we now turn to particular distributional assumptions. These examples allow us to derive more precise implications on the behavior of information costs, and to analyze the specific role of the distribution of information.

### 3.2 Role of the distribution of information

We characterize the certainty equivalent rate for two fundamental cases, central to the asset pricing literature, geometric Brownian motions and Poisson jumps, and compare their properties.

**Example 1.** (Brownian motion) Assume the following law of motion: \( \frac{dX_t}{X_t} = \sigma dZ_t \), with \( \{Z_t\} \) a standard Brownian motion, and volatility \( \sigma \). The certainty equivalent rate \( v(T) \) is the unique solution to

\[
\exp \left( v(T) T \right) = \frac{1 + \theta \Phi \left( \frac{\sqrt{T}}{\sigma} \left( v(T) - \frac{1}{2} \sigma^2 \right) \right)}{1 + \theta \Phi \left( \frac{\sqrt{T}}{\sigma} \left( v(T) + \frac{1}{2} \sigma^2 \right) \right)} < 1,
\]

where \( \Phi \) is the cumulative normal, and \( \theta \) is the coefficient of disappointment aversion.
The certainty equivalent rate $v(T)$ is increasing in the observation interval $T$, decreasing in the disappointment aversion $\theta$, and decreasing in the volatility $\sigma$.

Figure 1: Lottery values for a diffusion process: role of observation interval $T$, volatility $\sigma$ and disappointment aversion $\theta$.

Figure 1 illustrates the instantaneous rate $v$, in the case of a Brownian motion, as it varies with the parameters.

**Example 2.** (Poisson jumps) Assume $\frac{dX_t}{X_t} = \lambda \sigma dt - \sigma dN_t$, where $N_t$ is the counting variable for a Poisson process with intensity $\lambda$, and the jump fraction is $\sigma < 1$. The certainty equivalent rate $v(T)$ is the unique solution to:

$$\exp(v(T)T) = \frac{1 - \frac{\theta}{1+\theta} \frac{\Gamma(k+1,(1-\sigma)\lambda T)}{k!}}{1 - \frac{\theta}{1+\theta} \frac{\Gamma(k+1,\lambda T)}{k!}},$$

where $\Gamma(.,.)$ is the upper incomplete gamma function, and $k \in \mathbb{N}$ is the unique solution.
for:

\[
\frac{(v(T) - \lambda \sigma) T}{\log(1 - \sigma)} - 1 \leq k \leq \frac{(v(T) - \lambda \sigma) T}{\log(1 - \sigma)}.
\]

The certainty equivalent rate \(v(T)\) is increasing in the observation interval \(T\), decreasing in the disappointment aversion \(\theta\), and decreasing in the jump size and intensity \(\sigma\) and \(\lambda\).

Figure 2: Lottery values for a jump process: role of observation interval \(T\), disappointment aversion \(\theta\), jump size \(\sigma\) and intensity \(\lambda\).

Figure 2 illustrates the instantaneous rate \(v\), in the case of jumps, as it varies with the parameters.

These two fundamental examples allow us to draw insights on the general properties of information costs. As the fundamental risk of the lottery increases, information costs increase at all frequencies. Further, in our two examples, the average information cost \(-v(T)\) is decreasing in the observation interval: the more frequent the information, the more the agents want to stay away from the risky lottery. This
monotonicity property is stronger than the subadditivity of Proposition 2 and we conjecture it holds for arbitrary Levy processes. Geometric Brownian motions and jump processes have similar long-run behavior, and, accordingly, the risk-aversion contribution to the valuation of risk, i.e. the asymptotic behavior of \( v(T) \) as \( T \) goes to infinity, is the same under both processes.

However the local evolutions of diffusions and jumps are sharply distinct, which is reflected in the information aversion contribution to valuation. For the case of a Brownian motion, as the period of observation \( T \) tends to 0, the instantaneous certainty equivalent rate \( v(T) \) satisfies:

\[
v(T) = \frac{-\kappa(\theta) \sigma}{\sqrt{T}} + o\left(-\frac{1}{\sqrt{T}}\right),
\]

where \( \kappa(\theta) \) is positive, increasing in \( \theta \), with limit 0 in 0. As the frequency of information increases towards its continuous limit, the value of the lottery converges to 0, the worst possible outcome for the final payoffs, with a faster convergence the higher the coefficient of disappointment aversion \( \theta \), and the underlying risk \( \sigma \). To understand this result, keep in mind that, even though the agent’s time horizon does not change with the frequency of information, she evaluates her utility each time she observes a signal, and, under Brownian risk, is almost surely disappointed no matter how small the time interval. As the time interval becomes smaller and smaller, the information aversion contribution to the valuation of the risky asset dominates more and more, and, at the continuous information flow limit, mimics an infinite risk aversion. An alternative way to describe this phenomenon is through the lenses of the myopic risk aversion of Benartzi and Thaler (1995). The first-order risk aversion effect, inherent to preferences with kinks, results in agents who are more averse, comparatively, for small risks than for large risks. A frequent re-evaluation of the lottery value, when information arrives at small time intervals, corresponds to an accumulation of small risk taking. Because agents are first-order risk averse, a repetition of small risks is more costly for their utility than one large risk taking, and the lottery value decreases as the frequency increases.

In contrast, for the case of a jump process, the certainty equivalent rate has a
finite limit as the observation interval $T$ tends to 0, given by
\[ v(T) = -\theta \sigma \lambda + \mathcal{O}(T). \]

This result draws a sharp contrast between jump and diffusion processes. The difference is intuitive. With continuous information under a diffusion process, in any interval of time, there is an infinity of disappointing draws localized closely to the certainty equivalent, and priced with first-order risk aversion. Along the path of the jump process on the other hand, there is only a finite number of disappointing large draws, priced far from the kink and first-order risk aversion.

The strong differentiation across distributions in the continuous information limit is informative in terms of actual predictions. Under both processes, information aversion makes the valuation of risky assets decrease with the frequency of information, in line with the experimental evidence, however, one should expect more inattention to signals for which the value moves continuously than to those that display large sudden jumps. For instance, stock prices are subject to a lot of local variation, and our model implies, as is observed, that most investors do not monitor these small variations continuously. However, stock markets are also subject to large variations, or jumps, and the evidence (e.g. newspapers headlines) suggests investors are willing to pay attention to such shocks.

The results of this section provide a precise characterization of the costs of information flows. In our analysis so far, no informed action could affect, and improve, the payoff distribution. While this exercise allows us to relate to the experimental evidence, in practice agents collect information so as to make appropriate choices. The benefits of information must be accounted for, as highlighted by Beshears et al. (2012), who show the results of the lab experiments cited above cannot be replicated in a natural setting. We analyze how agents trade off the endogenous information costs we just described with the benefits of informed decision-making in the following section.
4 Optimal information decisions

When information can help in the decision-making, even information averse agents potentially choose to access it. In this section we study optimal information decisions, as well as how they interact with real allocation decisions, in a setup where information is instrumental. We consider a fundamental problem: the decision to consume and save, allocating savings between risky and risk-less assets. We relate the predictions of our model to the expanding body of evidence on how households manage and pay attention to their savings. But the insights we draw are not limited to this particular problem and can apply to any situation where information and risk-taking decisions interact.

First, we set up the consumption and savings problem, and characterize optimal decisions and their relation to the empirical literature. Second, we consider how exogenous shifts in information affect risk-taking. We find a more subtle interaction than suggested by the analysis of the previous section.

4.1 Consumption and savings problem

We consider a standard consumption and risky savings problem following the classic setup of Merton (1969). We assume the investor has recursive disappointment averse preferences and allow her to close her eyes and not observe the value of her portfolio for arbitrary periods of her choice. The basic structure of the optimal policy we obtain is similar to models in which inattention stems from exogenous fixed costs of information, e.g. Duffie and Sun (1990) or Abel et al. (2013). We emphasize the distinct predictions due to our endogenous, preference-based, foundation of the costs of information flows.

4.1.1 Preferences

We extend our definition of preferences to allow for intermediate consumption. To do so, we follow Epstein and Zin (1989), with a risk adjustment driven by disappointment aversion. We focus on a continuous-time setting as in Duffie and Epstein (1992). Heuristically, the value function $V_t$ for an information structure corresponding to the
filtration \( \{\mathcal{F}_t\}_{t \in [0, \infty)} \) and an adapted consumption process \( \{C_t\}_{t \in [0, \infty)} \) is the solution to the recursion
\[
V_t^{1-\alpha} = C_t^{1-\alpha} dt + (1 - \rho dt) (\mu_{\theta} [V_{t+dt} | \mathcal{F}_t])^{1-\alpha}.
\]
The parameter \( \alpha > 0 \) controls the elasticity of intertemporal substitution between consumption at different times, \( \rho > 0 \) is the rate of time discount. The only source of instantaneous risk aversion comes from the disappointment aversion operator \( \mu_{\theta} \). Our modeling choice readily invites comparisons to the commonly used version of the recursive utility model, in which risk-aversion is determined by the CRRA operator \( E (\cdot)^{1-\gamma} \gamma \), \( \gamma > 0 \), and we do so in the analysis that follows.

If the agent consumes deterministically over an interval of length \( T \) along which no information is revealed, the value function recursion takes the simple form:

\[
V_t^{1-\alpha} = \int_0^T e^{-\rho \tau} C_{t+\tau}^{1-\alpha} d\tau + e^{-\rho T} (\mu_{\theta} [V_{t+T} | \mathcal{F}_t])^{1-\alpha}.
\]
(5)

4.1.2 Opportunity sets

The opportunity set of the agent is constituted of two elements: allocation decisions and information decisions.

**Investment opportunity set** At each date, the agent can use her wealth \( W_t \) to consume or save. She has access to two investment accounts to allocate her savings: a risk-free asset with constant continuously compounded interest rate \( r \), and a risky asset with price determined by a stochastic process \( X \), with i.i.d. growth as in Section 3. We still write \( g \) the expected growth rate of the price of the risky asset and \( v(T) \) the certainty equivalent rate. To ensure finite utility, we assume \( r, g < \frac{\rho}{1-\alpha} \). The agent can rebalance her wealth across assets at all time, at no transaction cost. However, we do not allow for borrowing, so the agent cannot lever up. If the asset price can drop to 0, this assumption corresponds to the natural borrowing limit. Note \( S_t \) the number of shares of the risky asset owned at date \( t \). The agent’s sequence budget constraint
is
\[
\begin{align*}
    dW_t &= -C_t dt + S_t dX_t + r(W_t - S_t X_t) dt \\
    W_0 &= W, \ W_t \geq 0.
\end{align*}
\] (6)

**Information choice** The agent controls the information she receives by choosing when to open or close her eyes. Precisely, at any time \( t \) the agent decides either to receive no information, or to observe the full value of her risky portfolio, which she can do at no exogenous cost. In between observations, she makes decisions based on the last information she collected. Note this assumption does not correspond to limiting the cognitive ability of the agent, nor to assuming non-bayesian updating: the agent can always choose to access and process the maximal information available in the economic environment, and her expectations are driven by a standard increasing probabilistic filtration.

Formally, noting \( \tilde{\mathcal{F}}_t \) the filtration generated by the process \( \{X_t\} \) appropriately completed and \( \mathcal{F}_t \) that of the agent, the constraint on information is:

\[
\forall \ t, \mathcal{F}_t = \tilde{\mathcal{F}}_{\tau(t)},
\] (7)

\( \tau(t) \leq t, \text{ increasing, càdlàg.} \)

**4.1.3 Optimization problem**

Given initial wealth \( W \), the agent optimally chooses her filtration \( \{\mathcal{F}_t\} \) as in Equation (7), and her consumption and savings \( \{(C_t, S_t) \in \mathcal{F}_t \ - \text{ measurable}\} \), in order to maximize the value function of Equation (5) under the budget constraint of Equation (6).

Because the value function is homogenous of degree 1, and the opportunity set is linear in the total wealth, and identical at all time, we can rewrite

\[
\mathcal{V}(W) = W \mathcal{V}_0 (\{\mathcal{F}_t\})
\]

where \( \mathcal{V}_0 \) solely depend on the information choice, and not on the initial value of wealth. Information acquisition optimally happens at constant time intervals: at each observation, only the value of wealth changes, while the optimization problem for \( \mathcal{V}_0 \)
remains the same. The recursive structure of the opportunity set and preferences guarantees time consistency in the optimal policy. We note $T$ the optimal length of time interval, and $V_0(T)$ the value function for a unit of wealth.

At any time $t$ at which the agent observes her wealth, her optimization problem simplifies to choosing: i) $T$, the time until her next observation; ii) $\{C_{t+\tau}\}_{\tau=0}^{T}$, her deterministic consumption per unit of wealth between $t$ and $t+T$; and iii) $S_0$ her risky investment per unit of wealth.

We note $C_0 = \int_0^T e^{-r\tau} C_{t+\tau} d\tau$ the amount put in safe assets strictly to finance consumption between $t$ and $t+T$.

### 4.2 Optimal risk-taking and attention decisions

We derive the optimal risk-taking and attention policies. This characterization allows us to better understand the interaction between attention and risk-taking, and, further, to obtain clear predictions on conditions propice to inattention.

#### 4.2.1 Optimal strategy

**Proposition 3.** Given the observation interval $T$, the optimal consumption and savings strategies are:

$$
\begin{align*}
C_0 &= 1 - \exp \left[ \left( -\frac{\rho}{\alpha} + \frac{1-\alpha}{\alpha} v(T) \right) T \right], S_0 = 1 - C_0 \quad \text{if } v(T) > r \\
C_0 &= 1 - \exp \left[ \left( -\frac{\rho}{\alpha} + \frac{1-\alpha}{\alpha} r \right) T \right], S_0 = 0 \quad \text{if } v(T) \leq r,
\end{align*}
$$

(8)

where $v(T)$ is the certainty equivalent rate, when observing the stochastic process $X$ at intervals of length $T$, in the notations of Section 3.

The agent’s investment strategy, for her wealth remaining once her deterministic consumption is accounted for, is in a corner solution: she is invested either solely in the risk-free asset, or solely in the risky asset. When $v(T) > r$, the portfolio problem, across observations, is equivalent to having standard isoelastic utility and a deterministic rate of return $v(T)$, and the optimal consumption takes the simple form of

---

17 This feature arises naturally in our setting, whereas the literature on exogenous cost often needs to assume costs scale with wealth, e.g. Duffie and Sun (1990).
Equation (8). In particular, current consumption is increasing in the rate of return \( v(T) \) if and only if the elasticity of intertemporal substitution \( 1/\alpha \) is lower than 1, in which case the income effect dominates: facing a better opportunity set the agent consumes more immediately. Conversely, when \( 1/\alpha > 1 \) the substitution effect dominates: the agent pushes her consumption towards the future.

Before turning to the optimal attention decision, let us study how attention and risk-taking interact. Precisely, suppose exogenous changes are imposed on the observation interval, and consider how they affect investment in the risky asset. From Proposition 2, as long as expected returns on the risky asset exceed the risk-free rate, \( g > r \), there exists a threshold for the observation interval over which \( v(T) > r \) so the agent only invests in the risky asset. If the interval \( T \) decreases, the risky asset becomes less appealing as it involves receiving more and more information, possibly to the point where the agent can opt to exit the risky market: she reduces her risky position (to zero) when \( T \) decreases. However, as long as \( T \) remains high enough that \( v(T) > r \), a second opposing force affects her risky position when \( T \) varies. If the observation interval decreases, the risky asset may well become less and less appealing but the investor spends shorter periods of time without knowing the value of her portfolio so, in order to finance her consumption between observations she has to put away a smaller fraction of her wealth in the risk-free asset: she has room to increase her risky investments. In our setting where investment is in a corner solution, this second force always dominate. Therefore the observation in field experiments, as in Beshears et al. (2012), that investors do not reduce their risk-taking when receiving more information, is consistent with our framework as well. The insight that more information does not always induce less risk-taking for an information averse agent extends beyond our particular portfolio problem. While additional information is painful, if the agent receives it (as an optimal choice, or through external forces), she may as well take advantage of it and take better actions, potentially by engaging in more risk-taking.

We now characterize the optimal observation interval \( T \), when the instantaneous growth rate of the risky investment asset is greater than the risk-free rate, \( g > r \).\(^{18}\)

\(^{18}\)If \( g \leq r, v(T) \leq r, \forall T \), by a standard risk-aversion argument, and the problem admits \( C_0 = 1, T = \infty \) as a trivial solution.
Proposition 4. When $g > r$, the agent optimally observes her wealth at constant intervals of length $T^*$, where $T^*$ is such that $v(T^*) > r$, and the solution to:

$$
\frac{\partial v(T^*)}{\partial \log(T)} = \left( \frac{\rho}{1 - \alpha} - v(T^*) \right) \left[ 1 - \frac{f \left( \frac{\rho}{1 - \alpha} - r, T^* \right)}{f \left( \frac{\rho - (1 - \alpha)v(T^*)}{1 - \alpha} - v(T^*), T^* \right)} \right]
$$

(9)

where $f(x, T) = x / \left( \exp \left( \frac{1 - \alpha}{\alpha} x T \right) - 1 \right)$.

At the optimum, the following approximation obtains: 19

$$
\frac{\partial v(T^*)}{\partial \log(T)} \approx \frac{1}{2} \frac{1 - \alpha}{\alpha} T^* \left( \frac{\rho}{1 - \alpha} - v(T^*) \right) \left( v(T^*) - r \right).
$$

(10)

The right-hand side of Equation (9) represents the opportunity cost incurred when setting wealth aside for consumption at the risk-free rate $r$ rather than at the superior risky rate $v(T)$: it formalizes the benefits of information, and is standard to models with infrequent transactions à la Baumol-Tobin. In our framework, it is increasing in the observation interval $T$ both directly, and through the certainty equivalent rate $v(T)$.

The novelty of our approach is to make the marginal benefit to inattention, the left-hand side of Equation (9), endogenous. The downside to receiving more information is not determined by an ad-hoc exogenous fixed cost, but by the elasticity of the certainty equivalent rate $v(.)$, with respect to the observation interval $T$. This quantity reflects how much the agent lowers the valuation of her risky portfolio, and thus of her wealth, when faced with more numerous observations.

The approximation of Equation (10) gives rise to interesting interpretations. First, observe, under the “standard” recursive utility model, with a CRRA certainty equivalent on the continuation value, information benefits increase linearly in $T$, and there are no endogenous costs (since $v$ does not depend on $T$, it has elasticity zero). The “standard” recursive utility agent would thus simply observe her wealth continuously in our framework (as long as her certainty equivalent rate $v$ is greater than $r$), which makes clear the results we obtain under information aversion are unrelated to the

\[ \frac{\rho - (1 - \alpha)r}{\alpha} \approx 0 \] and \[ \frac{\rho - (1 - \alpha)v(T^*)}{\alpha} \approx 0 \] with same order of magnitude.
question of a preference for early or late resolutions of uncertainty. Second, as demonstrated in Section 3, the elasticity of the certainty equivalent rate \( v(.) \) with respect to \( T \) does not depend on the expected returns \( g \). An increase in expected returns, all else equal, unambiguously results in a decrease in the optimal length of time interval \( T^* \), under either endogenous or exogenous information costs. Third, under exogenously fixed information costs models, the optimal frequency of observations depends solely on the level for the certainty equivalent rate \( v \), whereas it depends on both the level and first derivative in our information aversion framework. Parameter changes that affect the slope but not the level of \( v \) have implications for the optimal frequency of information that can fully differentiate our endogenous costs model from the existing exogenous costs literature. To better understand what affects the elasticity of the certainty equivalent rate, we specialize to the case where the risky asset price follows a geometric Brownian motion.

### 4.2.2 The determinants of inattention

Consider the case of Brownian risk, with drift \( g \) and volatility \( \sigma \), as in Section 3. Figure 3 depicts the behavior of the value function and of the share of wealth allocated to the consumption account, as functions of the observation frequency, and highlights the existence and unicity of the optimal time interval between information acquisition.\(^{20}\)

To understand the determinants of inattention, we study the behavior of the unique optimal observation interval \( T^* \).

**Proposition 5.** The optimal attention interval \( T^* \), in the case of brownian returns, is

- **increasing in disappointment aversion \( \theta \),**
- **decreasing in expected returns \( g \),**
- **increasing in volatility \( \sigma \),**

\(^{20}\)The back-of-the envelope calibration of Figure 3 yields an optimal time interval of a little over 1 year, consistent with existing surveys. See for instance the 2003 survey by Unicredit Bank, and the 2004 Bank of Italy Survey of Households Income and Wealth, in Alvarez et al. (2012).
Figure 3: **Utility as a function of \( T \), the time interval between observations.**
For parameters values: \( \theta = 0.8, \alpha = 0.5, \sigma = 15\%, g = 10\%, r = 1\%, \rho = 0.2 \).

- increasing in volatility even when the certainty equivalent rate remains constant (through an increase in expected returns \( g \))

The intensity of information aversion affects the attention policy: more disappointment averse agents stay longer away from information. This prediction is consistent with the results of Alvarez et al. (2012), who find more risk averse investors check the value of their portfolios less often. Further, more volatile risky asset prices result in more inattention in our framework. Two elements drive this result: as volatility increases, the information flow is more intense, thus more costly; and the risky asset is less appealing because more risky. The first is specific to our approach; the second is also present in models of inattention with exogenous costs. Proposition 5 states inattention increases with the underlying risk even when expected returns increase together with volatility so as to maintain a constant valuation of the risky asset. This formal result differentiates our model from those with exogenous information costs. The stock market provides a natural setting to consider this implication. Sicherman
et al. (2014) document investors check the value of their investment accounts less often, when the VIX, an index of stock market volatility, increases. Because increases in volatility are, empirically, compensated by increases in expected returns, this evidence provides specific support for our approach.

5 Richer information choices

So far, we have considered the decisions of an investor with access to only the simplest tool to manage her information: choosing when to observe or not the value of her portfolio. While this setup is likely accurate for many investors managing their wealth, a finer access to information is possible with either the help of computers or the help of other agents. In this section, we study how to do so. We start by considering how the information flow can be better tailored to the agent’s specific preferences. Then we consider the scope for delegating decisions. The insights we develop here can be considered both from a positive and a normative point of view: providing a rationale for information systems used in practice, or suggesting ways to help agents deal with their information aversion.

5.1 Information delegation

Our framework makes possible the comparison of arbitrary structures of information flows. Information policies must simply satisfy the following two conditions: the filtration \( \{F_t\} \) must be increasing, to respect Bayesian updating and no-forgetting; it must be smaller than the maximum information available at date \( t, \bar{F}_t \)

\[
\forall t, \ F_t \subseteq \bar{F}_t, \ F_t \text{ increasing.} \tag{11}
\]

Given such a policy, one can determine the optimal allocation policy — consumption and savings in our model — and derive the value of wealth, including the endogenous costs of such an information flow. While this seems, at first glance, a straightforward extension to the problem analyzed in the previous section, it is one that fixed-cost models of information cannot address in a meaningful way. An investor might be in-
interested in seeing all her wealth at given intervals of time; and/or in receiving state-dependent signals telling her when her wealth reaches a certain threshold; and/or in checking at regular intervals if her wealth has gone up more or less than a certain percentage. These choices arguably entail different information costs. With exogenous costs models, in the style of Duffie and Sun (1990), these relative information costs can only be ascribed in an ad-hoc fashion. Under information aversion, on the other hand, each signal does yield a different cost, endogenously depending on how informative the signals are and on the risk-taking decisions the agent makes.

Rather than studying all the possible information structures satisfying Equation (11), we consider whether simple signals can help the investor. In addition to the time-dependent observations the agent can obtain on her own, and which we studied in the previous section, we include state-dependent alerts the agent receives when her risky account falls below a certain threshold. The following proposition shows alerts following poor performance do help the investor.

**Proposition 6.** When returns follow a Brownian motion, the agent is strictly better off if she can add to her regular full wealth observations a state dependent signal she observes only when her wealth falls below a pre-specified threshold of her choice.

The additional alert in bad times has three distinct effects on the investor. First, since the agent is information averse, more frequent information comes at a utility cost. Second, however, the additional information allows her to improve on her post-signal decision making, i.e. to adjust her consumption and portfolio in response to the bad news. Third, and more subtle, knowing she may receive additional information through an intermediate signal also impacts her ex-ante decision making. The signal acts as a backstop against running down the risky account. Because she knows she will be alerted before her risky account reaches 0, she can engage in more risk-taking by financing some of her consumption from the risky rather than the risk-free asset. For a low enough threshold and with Brownian returns, this last positive effect dominates. The utility gains from the increased risk-taking ex-ante are first-order in the threshold. On the other hand, both the ex-post reallocation gain as well as the information costs are of similar order as the probability of hitting the threshold; this
probability is of higher order in the threshold and therefore dominated.\footnote{This argument generalizes to other distributions where the probability of reaching a threshold close to 0 decreases fast enough with the threshold.}

The result of Proposition 6 highlights an insight that extends beyond our particular model of consumption and savings. Abel et al. (2013) find time-dependent rules to be optimal in a setting with fixed observation and transaction costs. In our setting with endogenous information costs, allowing for rich information structures, adding state-dependent rules dominates over pure time-dependent rules. Obtaining information precisely when it is needed is worth the additional utility cost.

In practice, the alarms we considered in this section are natural to implement: a broker or bank can easily contact their clients following poor portfolio performance. More generally, while staying away from news most of the time is valuable, becoming aware of extreme events is useful. The media representation of news, making large information arrivals unavoidable, is consistent with our result.

## 5.2 Decision delegation

To assist an information averse agent, one can go further and delegate allocations, thus removing the necessity to actively seek information. The investor in our model might want to ask a portfolio manager to take care of her savings. Delegation seems like the perfect tool against information aversion: pay somebody, or program a computer, to be fully informed and make all decisions, and you no longer have to look for information? Though intuitive it turns out to be partly false: delegated management cannot always shield the agent from receiving information, in particular in our consumption-savings model.

Adapting our framework to allow for delegated management is straightforward. We let decisions be taken according to all the information available, \( \tilde{\mathcal{F}}_t \). Quantities entering the current flow utility however must be observed by the agent, i.e. in the agent’s information set \( \mathcal{F}_t \): portfolio decisions can be made hidden from the agent,
consumption cannot. The measurability conditions are

\[ C_t \mathcal{F}_t \text{-measurable}, \] (12)
\[ S_t \mathcal{F}_t \text{-measurable}. \] (13)

These conditions make clear the benefits of delegation to erase information costs are limited in our framework: to better manage the investor’s wealth, the delegated manager must make consumption adjust with portfolio performance, thus automatically burdening the agent with information.

There are, however, cases in which delegated management can strongly mitigate information costs. Consider the following example. An investor whose only objective is to maximize her wealth at a final date \( \tau \), when she consumes, can invest in various risky and risk-free assets with observable time-varying expected returns. If she cannot delegate, the information averse investor will trade off the benefits of active portfolio management with the costs of information. If she could, on the other hand, she would delegate all portfolio management decisions and would only observe the final value of her wealth when she consumes at time \( \tau \). Delegation in this example can fully shield the agent from all information costs.

The key difference with our framework is the horizon at which the consequences of allocation decisions are realized. In our consumption-savings problem, delegated decisions concern consumption choices, and are immediately realized. With market-timing, delegated decisions concern portfolio allocations, and need not immediately impact consumption. These results provide some guidance as to when delegation should be observed in practice. Cases where optimal decisions’ implications are quickly observed, and cannot be bundled over time, limit the scope for delegation, in contrast to decisions with long-term implications only. Consistent with this argument, the delegation of active portfolio management of retirement accounts is common in practice, while short term consumption and saving decisions are typically made by the agents themselves.
6 Extensions

Even in a simple consumption-savings framework, we showed the endogenous informations costs of our model provide novel insights, with broad empirical support. Besides, our approach has pervasive implications for decision-making under uncertainty, relative to models with exogenous information costs or constraints, of which this is but one example. We briefly revisit below several classic questions, and stress the novel tradeoffs when agents are information averse.

6.1 Diversification and the multiplication of information flows

A robust insight of portfolio theory is that diversification is valuable. When presented with two assets with imperfectly correlated returns, it is optimal to invest in both. Because our disappointment averse agents are risk-averse, the rationale for diversification obtains. However, in our framework, not only does the distribution of the final payoffs matter, but also the structure of the information flow. It is plausible investing in a larger number of assets corresponds to more frequent arrivals of information, which might diminish and even overcome the benefit of diversification.

To characterize the tradeoff between the costs and benefits of diversification in our model, we study a simple example. Suppose the agent receives at date $\tau$ the final value $\lambda X^{(1)}_{\tau} + (1 - \lambda)X^{(2)}_{\tau}$, where $X^{(1)}$ and $X^{(2)}$ are two arithmetic Brownian motions with volatility $\sigma$ and correlation $\rho$, and $\lambda \in [0, 1]$ can be thought of as a portfolio share. Let the agent’s observations, at intervals of length $T$, alternate systematically between the two processes.

In Figure 4, we consider (a) investing in only one asset ($\lambda = 0$), (b) investing in two perfectly correlated assets ($\lambda = 50\%$, $\rho = 1$), and (c) investing equally in two fully independent assets ($\lambda = 50\%$, $\rho = 0$). Investments (a) and (b) share the exact same payoff structure, but have different information flows, with higher signal frequency for case (b), and thus a lower valuation. Investments (b) and (c) have same information flows, but different risk exposures: the diversified investment (c) yields a higher value. The most interesting comparison is between (a) and (c). In this particular example, when assets are perfectly uncorrelated, the diversification motive dominates over the information costs: the agent always prefers the diversified portfolio with fre-
Figure 4: **Role of diversification.** Certainty equivalent as a function of the observation interval for (a) a single asset portfolio (red), (b) an equal-weight perfectly correlated portfolio (green), (c) and an equal weight independent payoff portfolio (blue). For arithmetic Brownian motions with volatility $\sigma = 0.1$, and for $\theta = 1$.

...quent information (c) over the portfolio with one asset and infrequent information (a). The benefits of diversification, however, are greatly diminished by the multiplication of information flows. At higher frequency, in particular, as information costs increase, the agent is close to indifferent between holding a diversified portfolio with more information versus holding a single asset.

### 6.2 Leverage and information decisions

In Section 4, we prohibited the investor from taking on any leverage, which corresponds to the natural borrowing limit under time-dependent rules, since an agent with levered positions cannot avoid bankruptcy. On the other hand, if the asset price...
follows a geometric brownian motion, and if the agent observed it continuously, she could take arbitrary levered positions: levering up requires being and keeping informed.

As long as there is a finite (arbitrarily high) borrowing limit, an agent with access only to time dependent rules would not take any leverage. In the richer information filtrations set of Section 5, downturn alerts allow the agent to lever up into the attractive risky asset, without incurring the dissuasive cost of continuous information flows. Even then, though, the agent would not choose to lever up above a given level: the more levered her portfolio, the higher the threshold she needs to set for her downturn alerts, and the more frequent, and thus costly, they become.

Information aversion thus yields non-trivial interconnections between leverage decisions and attention decisions. The information costs due to the monitoring of levered positions are a likely complement to the margin costs emphasized by Mitchell et al. (2002).

6.3 Learning, information and risk-taking dynamics

Intuitively, for a given signal about a lottery, the information cost is hump-shaped in the quantity of information (see Corollary 1 and Corollary 3). This non-monotonicity has potentially rich implications for learning decisions.

As an illustration, take the framework of Section 4, and assume the agent does not know the growth rate $g$. She can learn about $g$ by observing her wealth (provided she invests a given portion of her wealth in the risky asset), and from independent signals she receives when she observes her wealth. If these signals are very informative, they are comparatively not very costly, and she would optimally observe them very fast in order to fully learn the value of $g$ and then adjust her information frequency down to the optimal one of Section 4. If they are not very informative, they are still not extremely costly, but observing her wealth is, so she might maintain a very low frequency dynamics, where only a small part of her wealth is invested in the risky asset, up to the point she learns $g > r$, and she switches her whole portfolio to the risky asset, and increases her observation frequency to the optimal one at steady-state. Finally, if the signals are in a middle range of informativeness, they might be
too costly, on their own to be worth observing, and in this intermediate region, the investor might fully abstain from investing in the risky asset.

This simple example illustrates the complex interconnections between learning, information and risk-taking, and their dynamics, when agents are information averse. The existence of no-learning regions would not only affect investment decisions, but could have broad implications in other areas of decision making where learning is key, e.g. the decision to engage in medical testing, to collect information and invest in a new technology etc.

6.4 The supply of information

In practice, information is produced and disseminated by agents or institutions. In an economy populated by information averse agents, suppliers of information need to adapt and appropriately tailor the flow of information. As such our model provides the basis for a theory of optimal opaqueness. While providing an in-depth treatment of this question is left for future research, we briefly outline a few simple implications.

One way to help information averse agents is to lump news together in bundles delivered at precise points in time. Such a behavior is consistent with firm’s disclosure policies organized around scheduled earnings announcement. Similarly, monetary policy is disclosed at precise points in time, at 2:00p.m. following FOMC meetings, most of which are scheduled in advance. Other macroeconomic announcements, such as employment numbers, quarterly growth etc., also follow discretely spaced releases. A more detailed examination of our framework could provide further guidance for the design of such information release policies.

Agents do not want to receive information too often. However, when they do observe information (either of their own choice or due to external forces), the result of Corollary 1 indicates they want it to be as precise and “transparent” as possible. Ours is a framework in which suppliers sometimes refraining from releasing any information can be beneficial; but suppliers releasing partial or distorted information is not.

\[23\] Acharya and Lambrecht (2014) provides an alternative theory of earnings target set to manage investors’ expectations.
Observe, further, even if this form of opaqueness is intrinsically desired by economic agents, it generates asymmetric information, and agency problems are likely to arise in those situations, e.g. between an investor and her wealth manager. These potentially counteract the motive for information withholding. To account for information aversion, optimal compensation contracts need to provide the necessary incentives, while minimizing the information needed to enforce them.

7 Conclusion

Because they run the risk of being disappointed each time they receive a signal, disappointment averse agents are intrinsically information averse. We propose a theory of inattention solely based on these preferences, absent any cognitive limitations, or external costs of acquiring information. We start by characterizing the strength and properties of the endogenous costs of information, implied by this model of preferences, and find them to differ fundamentally from both the cognitive constraints, and the exogenous costs commonly used in the inattention literature. We analyze the impact of the frequency of observations on the certainty equivalents of lotteries whose payoffs correspond to the final value of a stochastic process, and find our model justifies the experimental evidence that shows agents lower the valuation of risky assets when provided with more information. We then study how agents balance the utility cost of paying attention to the economic environment with the benefits of making informed decisions, and illustrate this trade-off in the case of a standard consumption-savings problem. In this setting, we find attention decreases in turbulent times: when there is more risk, information is more stressful. This endogenous cost-driven result is unique to our model of inattention, and is supported by the empirical evidence. We explore how to better tailor information filtrations to address information averse investors’ specific needs, and emphasize our model is uniquely equipped to analyze such a fundamental problem. We show state-dependent information strategies can improve on pure time dependent ones.

More generally, taking the point of view that people might fundamentally want to stay away from information draws a very different picture of inattention than standard models. Facilitating the access to information might be detrimental. This insight
has pervasive implications for decision-making under uncertainty. While we outline the interconnections between information choices and delegation, leverage, learning, and the supply of information, many questions remain. We believe the simplicity of our approach suggest a large avenue for future research, both to further clarify the theoretical predictions of our model, and to explore its rich empirical implications.
References


